

# Known and unknown neutrino mass-mixing properties



APC Paris  
France

Elgio Lisi

APC Colloquium, 9 April 2021

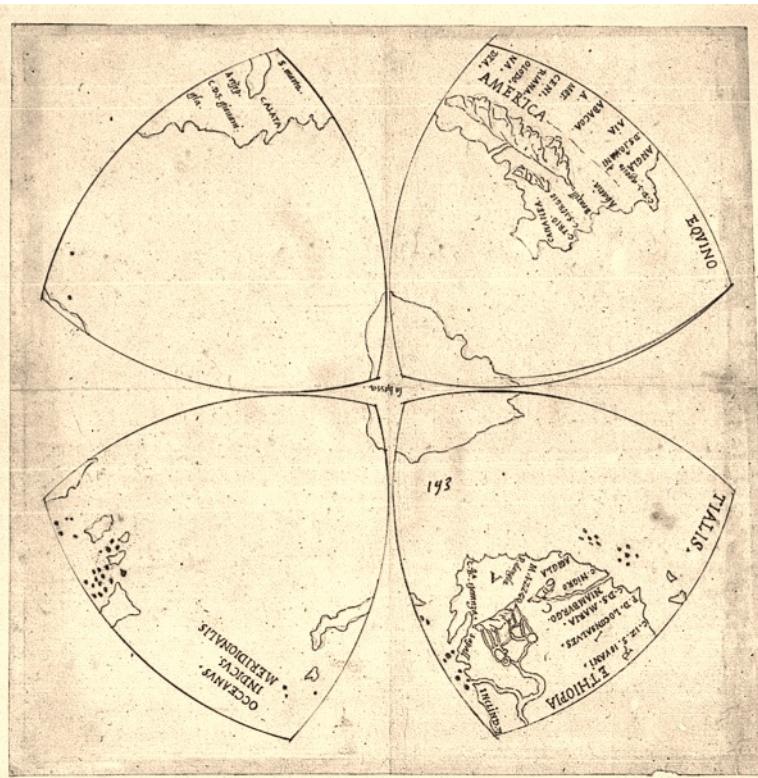


INFN Bari  
Italy

# PROLOGUE: A remarkable world map (~ 1514)...



Northern hemisphere

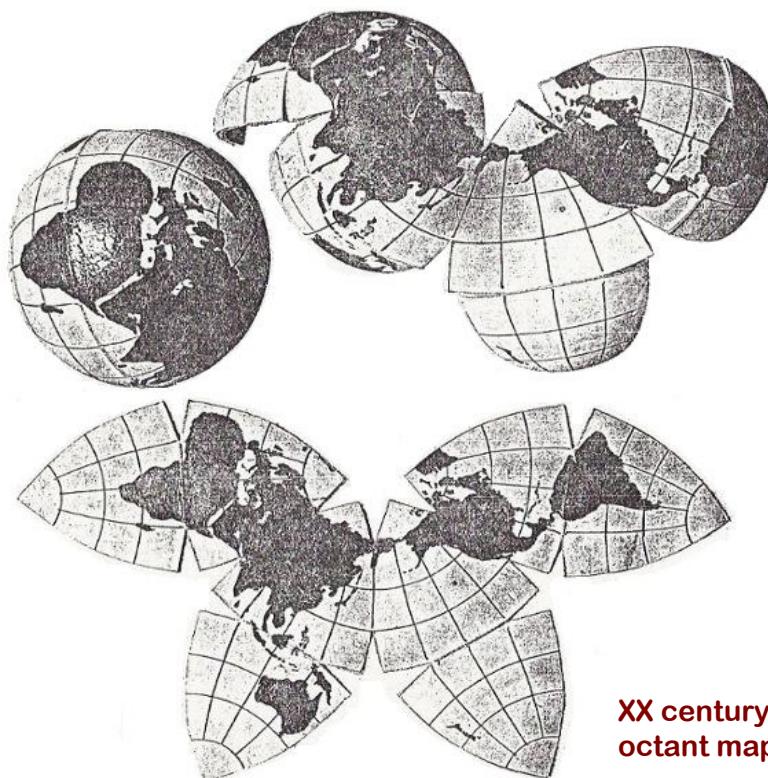
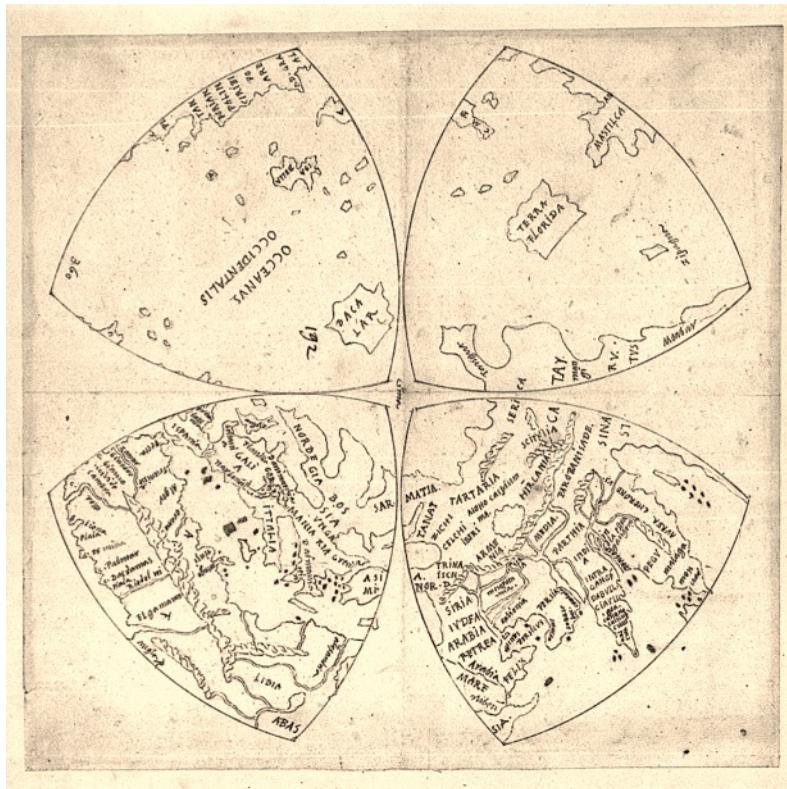


Southern hemisphere

... attributed to Leonardo da Vinci [1452-1519]

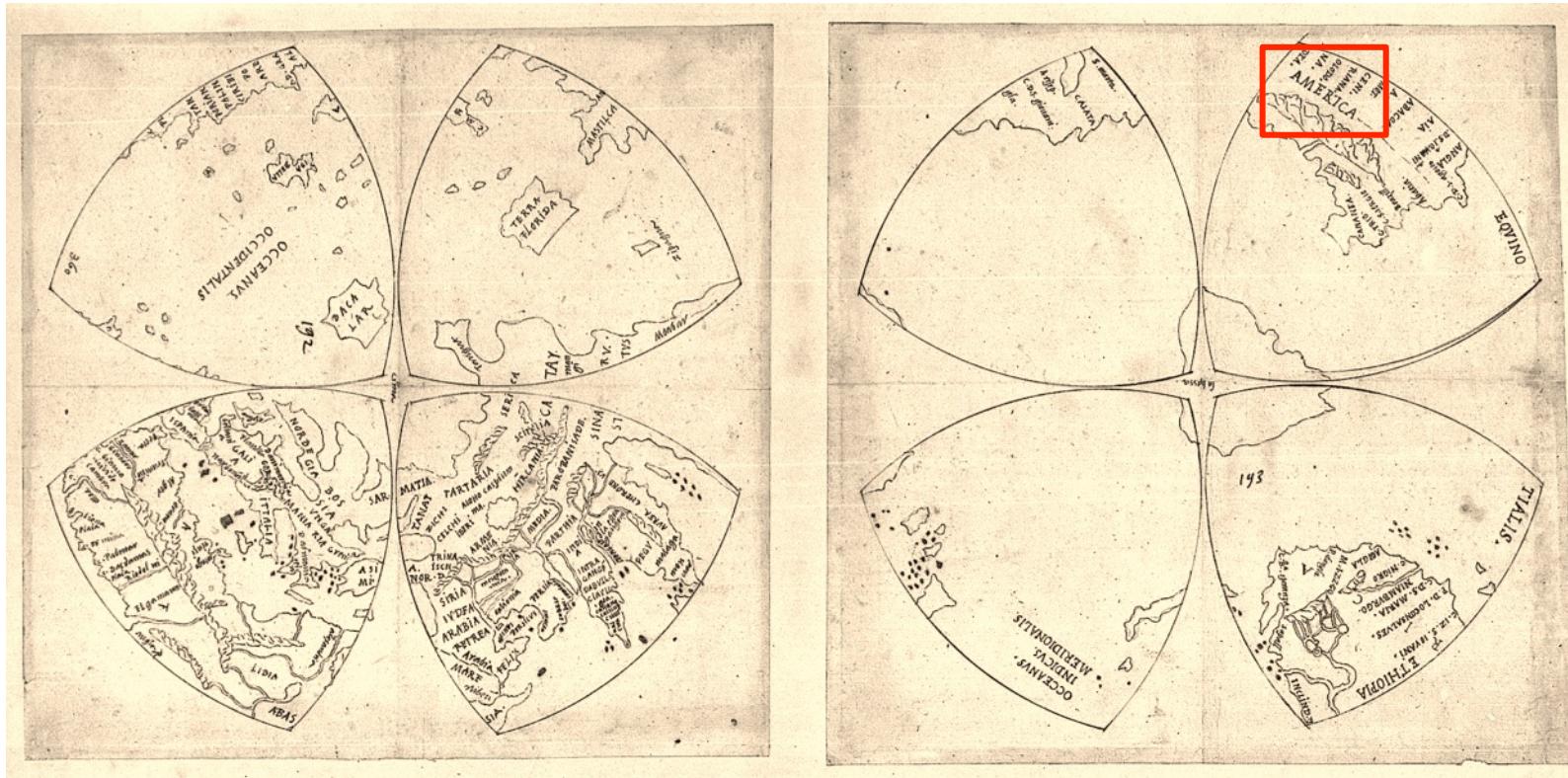
[Now at the Royal Library, Windsor Collection. Executed by one of Leonardo's assistants.]

# Earliest known world map ...



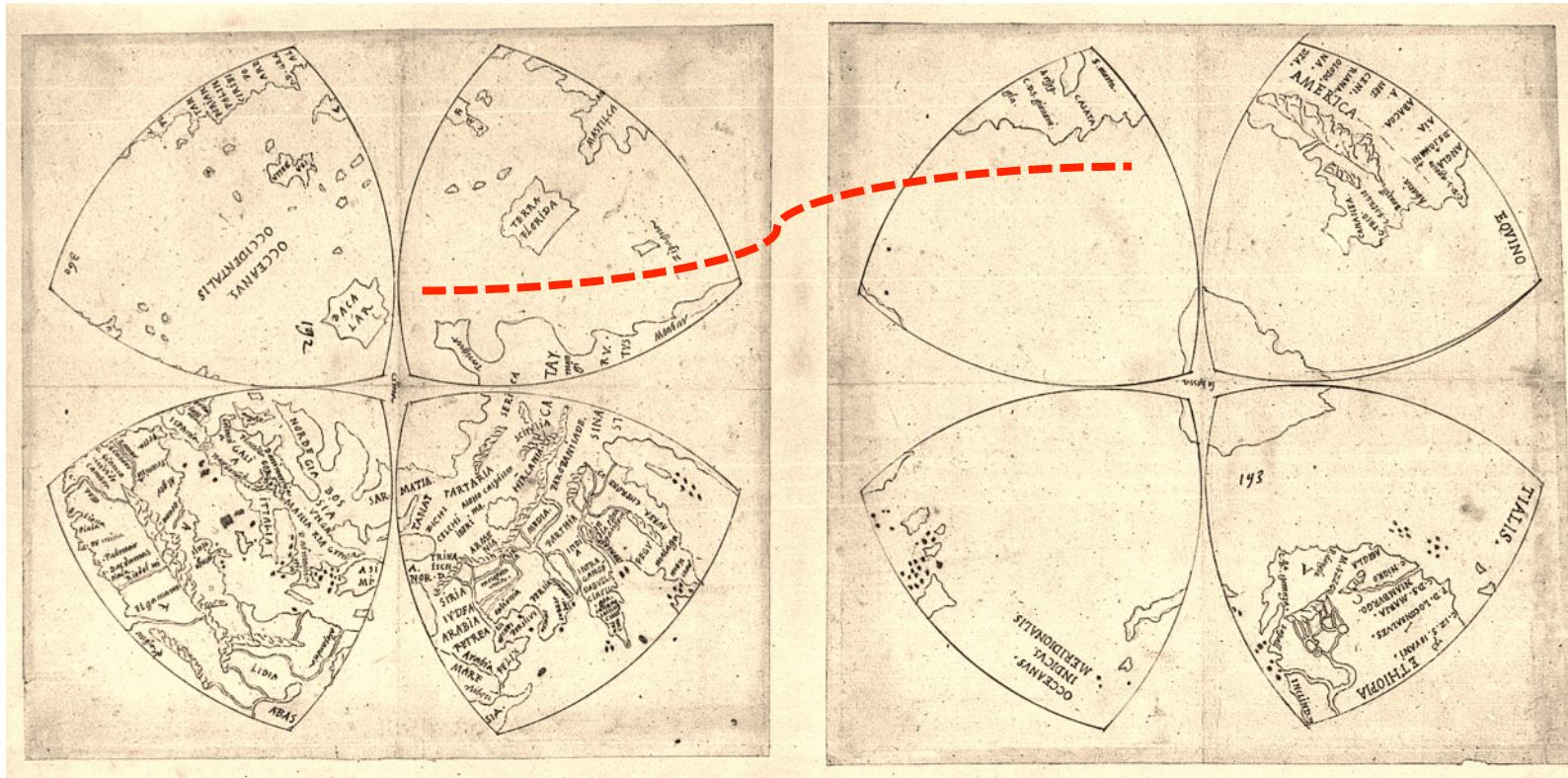
... made with octant projections (1/8's of the globe)

# Earliest known world map ...



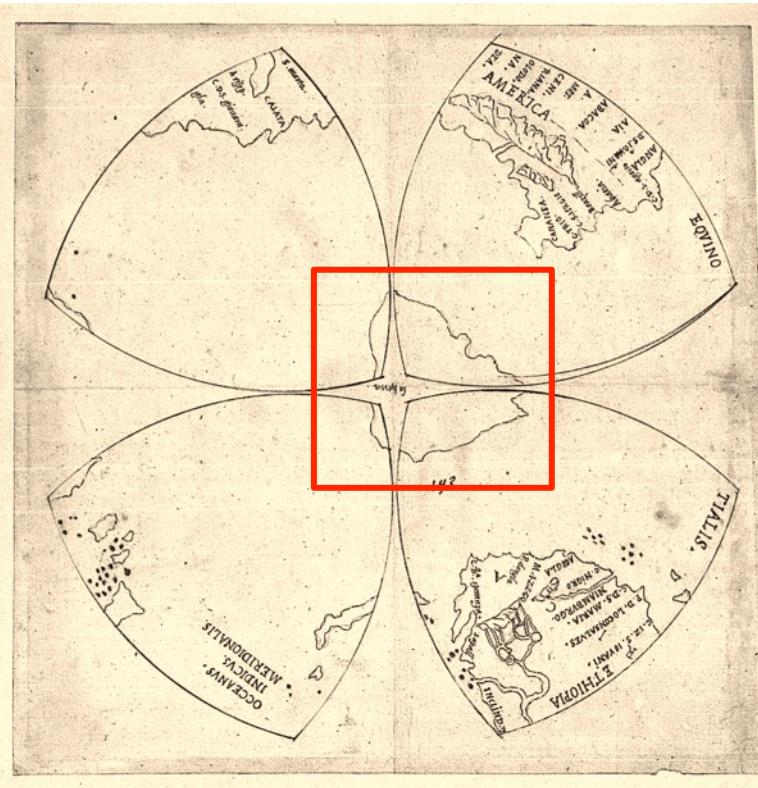
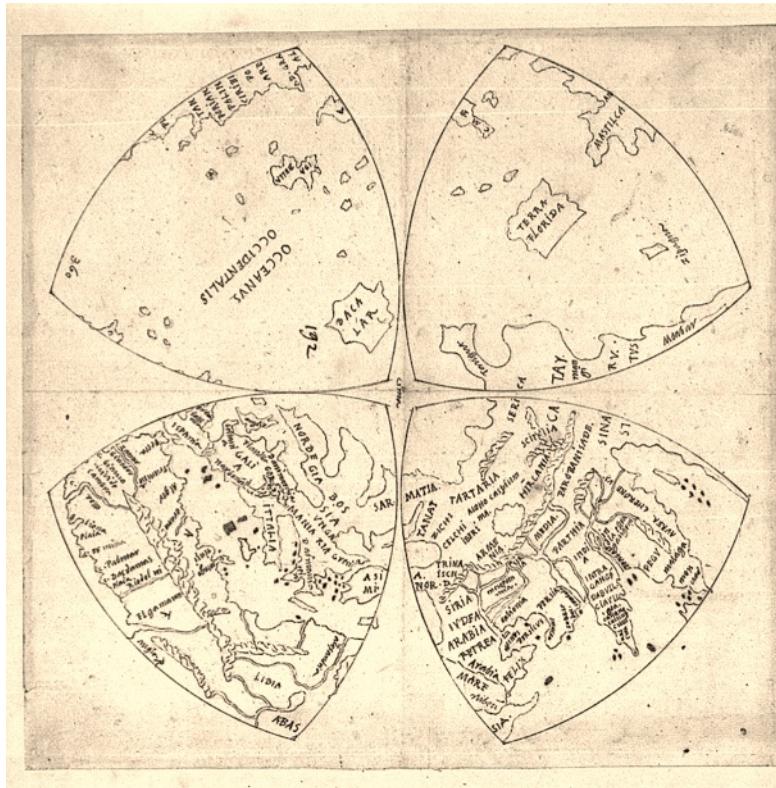
... made with octant projections (1/8's of the globe)  
... showing the name “America” for the New World

# Earliest known world map ...



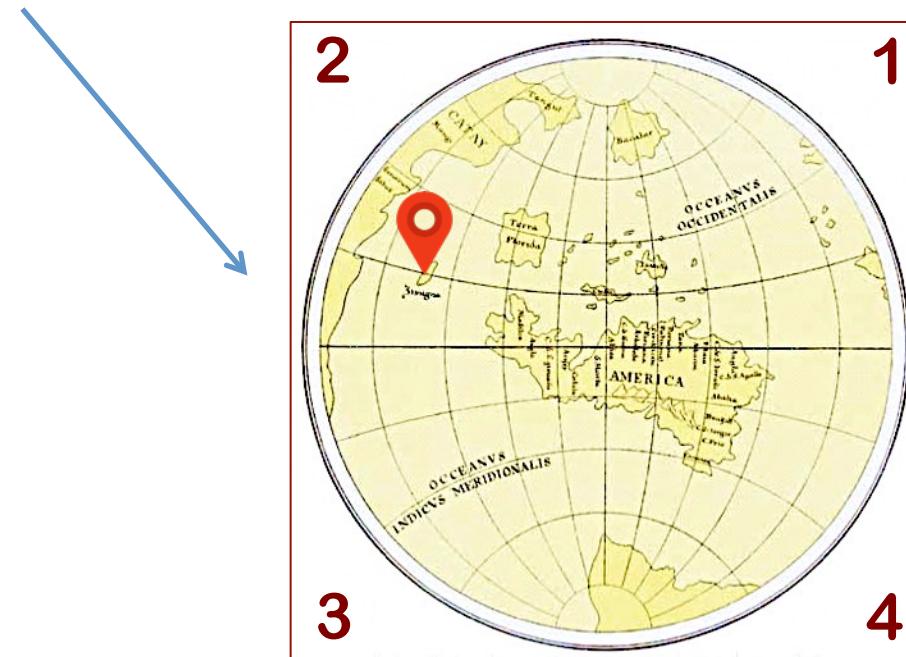
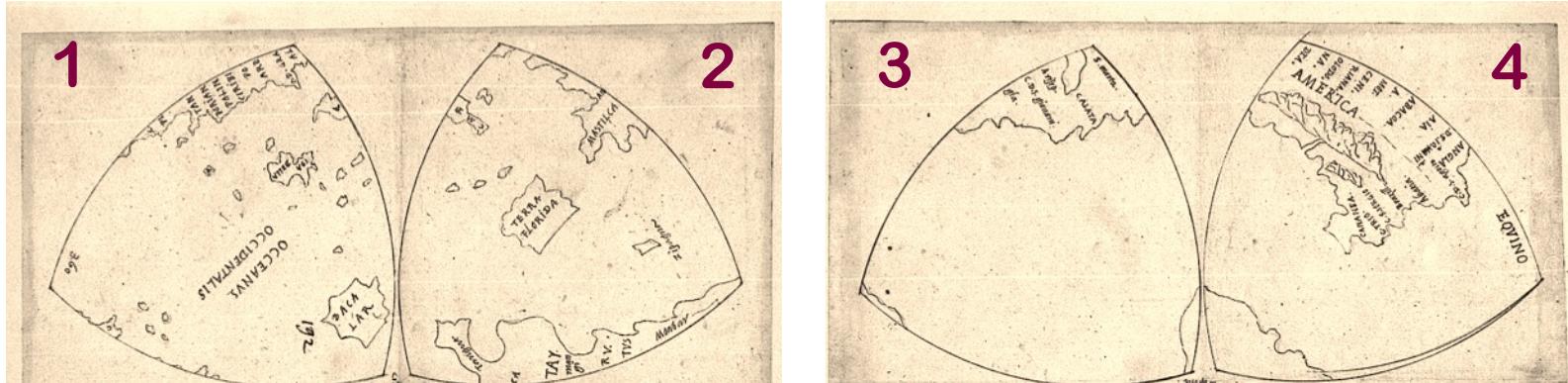
... made with octant projections (1/8's of the globe)  
... showing the name “America” for the New World  
... with America’s west coast disconnected from Asia

# Earliest known world map ...



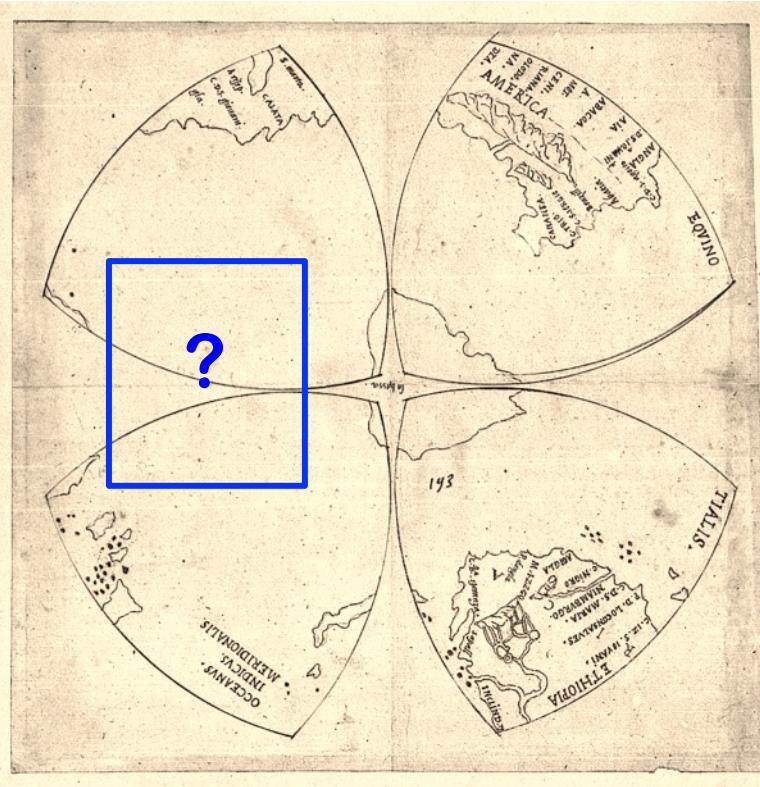
... made with octant projections (1/8's of the globe)  
... showing the name “America” for the New World  
... with America’s west coast disconnected from Asia  
... indicating a large Southern continent (a bold guess!)

# But Leonardo could not yet...



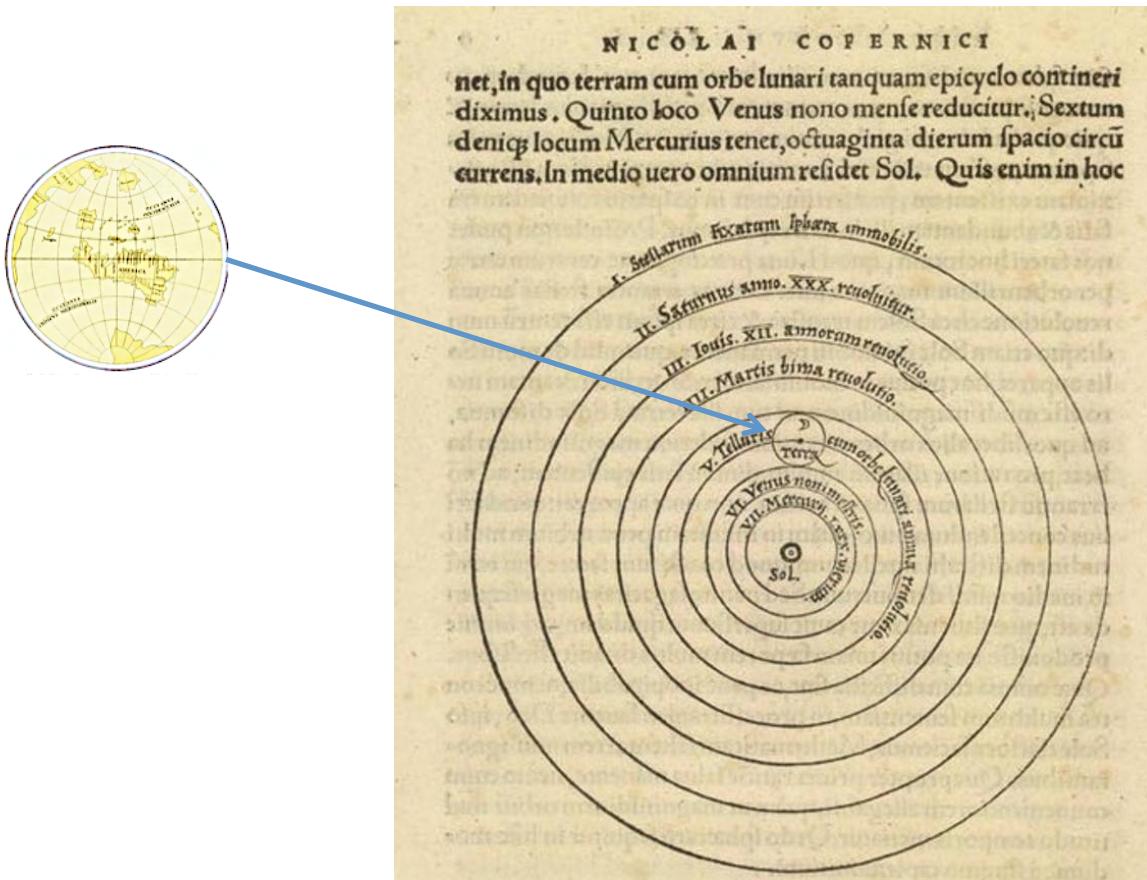
... avoid mapping distortions and biases

# But Leonardo could not yet...



... know about Australian continent (~ 90 years later)

**But Leonardo could not yet...**



**... fully grasp a bigger picture of the world  
(Copernicus, ~30 years later)**

After ~500 years...

...we are experiencing a similar situation in  $\nu$  physics:

- being excited by a series of discoveries
- charting the newly discovered territories
- trying to avoid distortions and biases
- seeking unknown lands and a bigger picture

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...we are experiencing a similar situation in  $\nu$  physics:

- being excited by a series of discoveries
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...which is also the thread of this Colloquium:  
an interplay between known and unknown neutrino properties

- being excited by a series of discoveries

## 1998: Annus Mirabilis for “APC”

“C”

accelerated expansion  
of the Universe

$$\rho_{\text{vac}} \sim (2 \times 10^{-3} \text{ eV})^4$$

“AP”

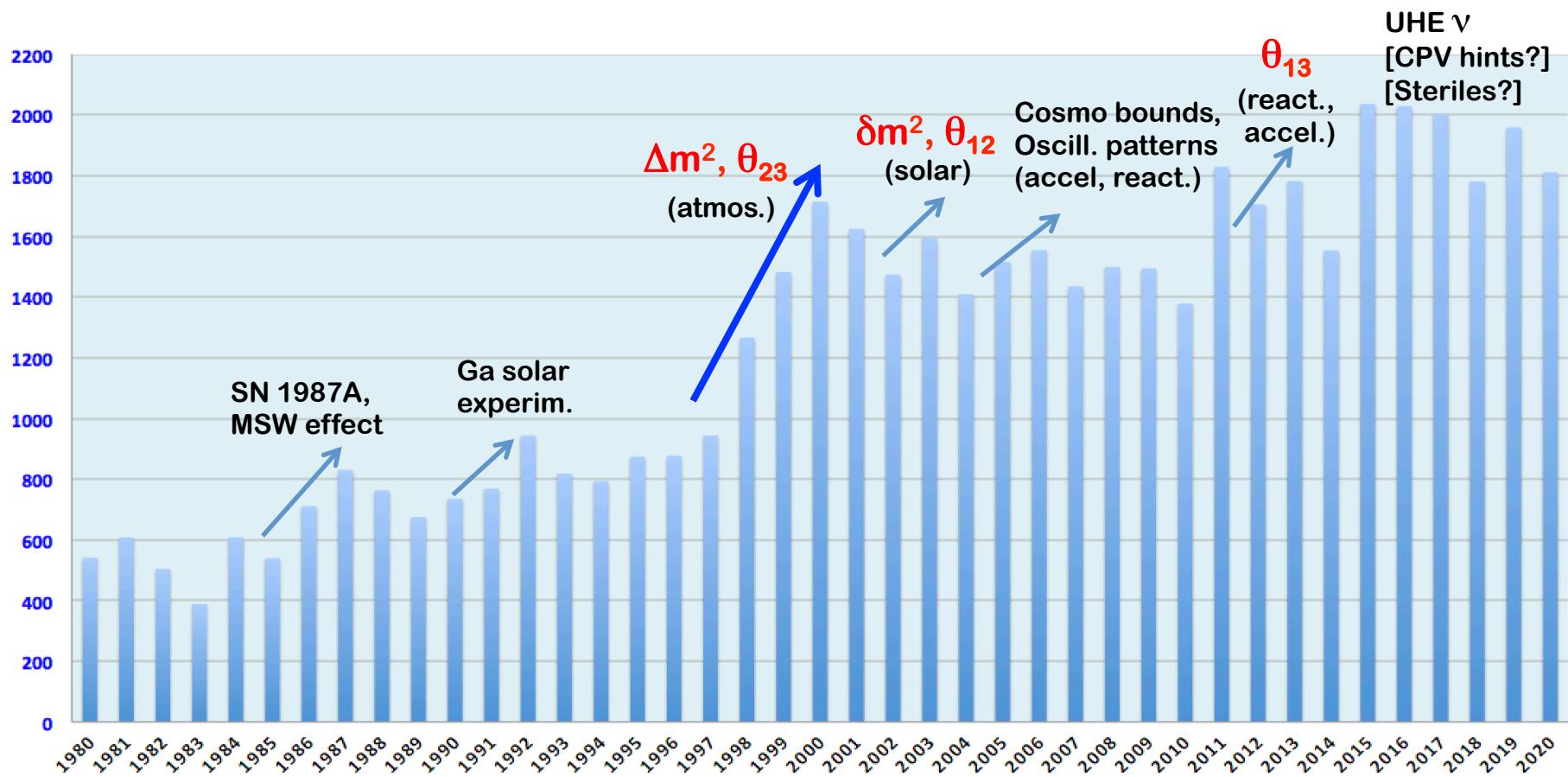
oscillations of  
atmospheric neutrinos

$$\Delta m_{\text{atm}}^2 \sim (5 \times 10^{-2} \text{ eV})^2$$

Evidence for dark energy

Evidence for neutrino mass

# Papers with \*neutrino\* in the title, 40-yr trend from INSPIRE HEP



$\Delta m_{ij}^2 L/E \sim$  oscillation phase in vacuum  
 $\sin^2 \theta_{ij} \sim$  oscill. amplitude in vacuum

$\nu_\alpha \rightarrow \nu_\beta$  (appearance)  
 $\nu_\alpha \rightarrow \nu_\alpha$  (disappear.)

→ standard ν paradigm established

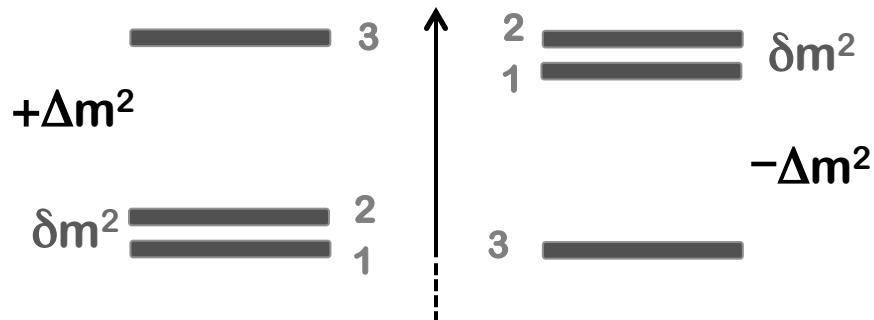
## The standard 3v paradigm: parameters

## Mixings matrix: CKM → PMNS (Pontecorvo-Maki-Nakagawa-Sakata)

## Mass [squared] spectrum

$(E \sim p + m^2/2E + \text{"interaction energy"})$

# “Normal” Ordering N.O.



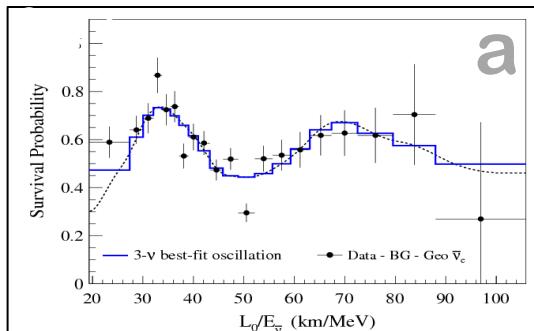
# “Inverted” Ordering I.O.

$$\delta m^2 = \Delta m_{21}^2, \quad \Delta m^2 = (\Delta m_{32}^2 + \Delta m_{31}^2)/2$$

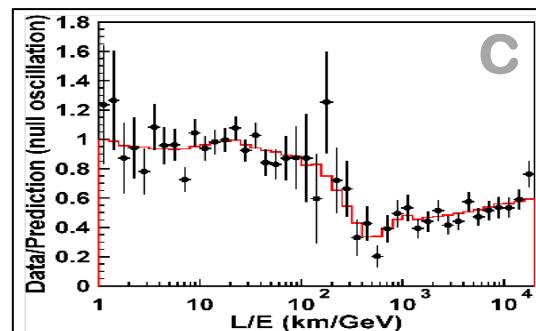
- + interactions in matter → effective terms  $\sim G_F \cdot E \cdot \text{density}$
- + absolute neutrino mass scale (not tested in oscillations)

# Beautiful $\nu$ oscillation data have established this 3 $\nu$ paradigm...

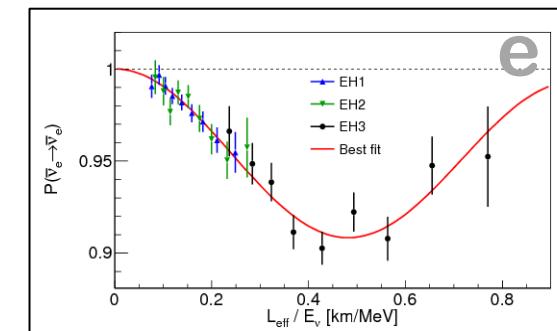
$e \rightarrow e$  (KamLAND, KL)



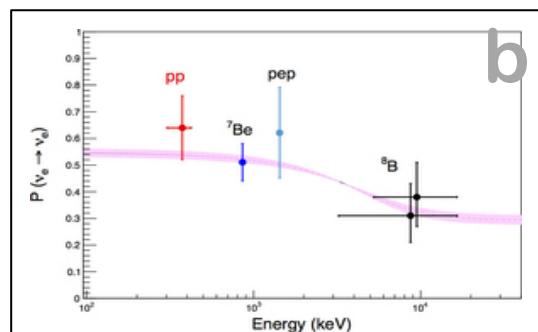
$\mu \rightarrow \mu$  (Atmospheric)



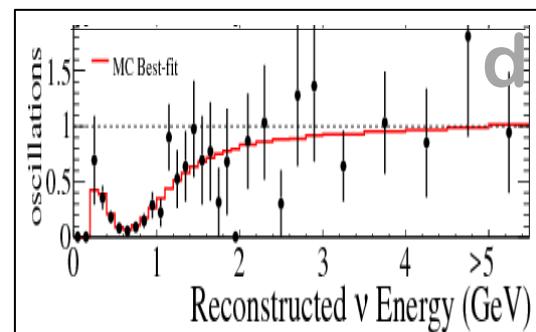
$e \rightarrow e$  (SBL Reac.)



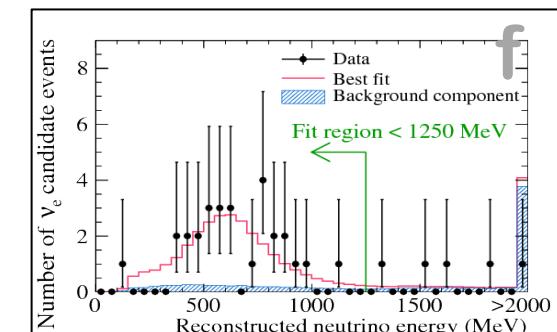
$e \rightarrow e$  (Solar)



$\mu \rightarrow \mu$  (LBL Accel.)



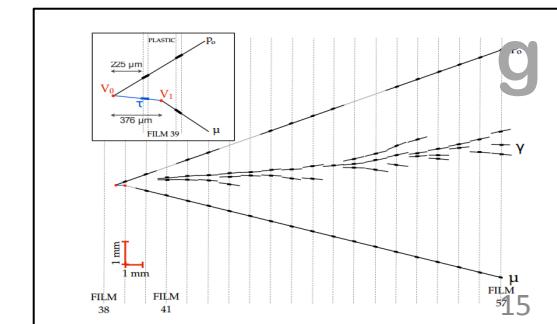
$\mu \rightarrow e$  (LBL Accel.)



LBL = Long baseline (few  $\times$  100 km); SBL = short baseline ( $\sim$ 1 km)

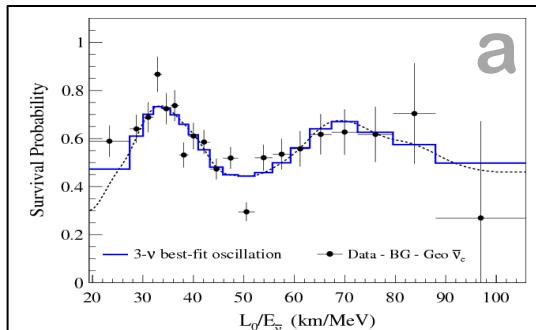
- (a) KamLAND reactor [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], DeepCore, MACRO, MINOS etc.; (d) T2K (plot), NOvA, MINOS, K2K LBL accel.; (e) Daya Bay [plot], RENO, Double Chooz SBL reactor; (f) T2K [plot], MINOS, NOvA LBL accel.; (g) OPERA [plot] LBL accel., Super-K and IC-CD atmospheric.

$\mu \rightarrow \tau$  (OPERA, SK, DC)

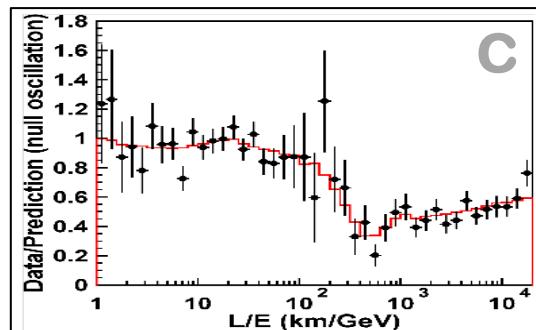


... and consistently measured five ν mass-mixing parameters

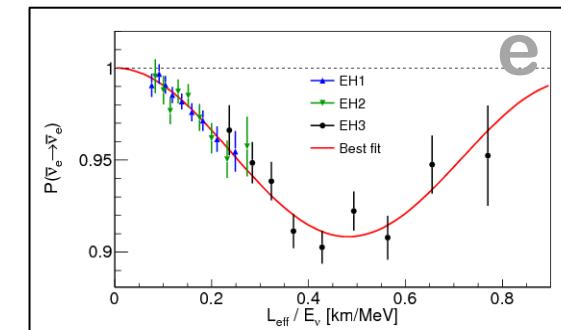
$e \rightarrow e$  ( $\delta m^2, \theta_{12}$ )



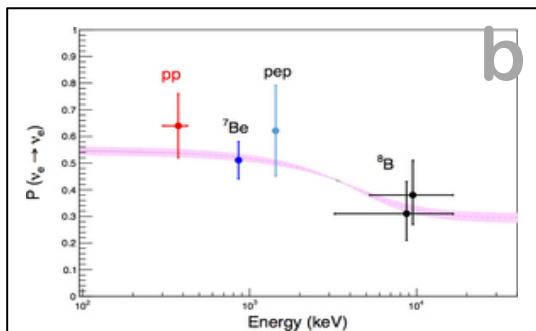
$\mu \rightarrow \mu$  ( $\Delta m^2, \theta_{23}$ )



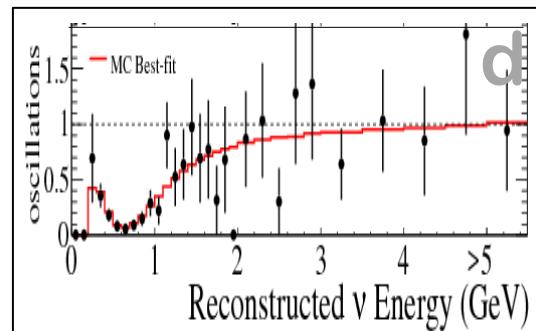
$e \rightarrow e$  ( $\Delta m^2, \theta_{13}$ )



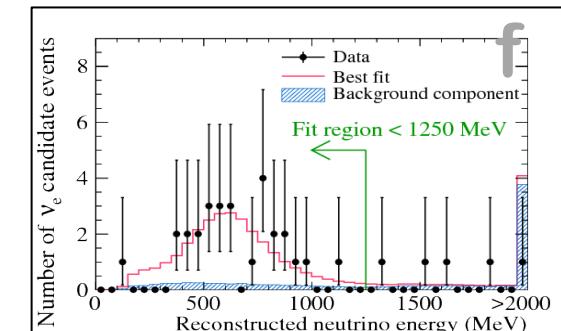
$e \rightarrow e$  ( $\delta m^2, \theta_{12}$ )



$\mu \rightarrow \mu$  ( $\Delta m^2, \theta_{23}$ )



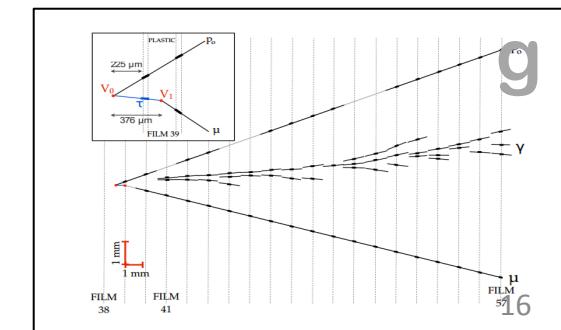
$\mu \rightarrow e$  ( $\Delta m^2, \theta_{13}, \theta_{23}$ )



Each leading oscillation parameters (over)constrained by at least two classes of measurements → 3ν consistency

Subleading effects involve CPV and NO vs IO difference, essentially via  $\mu \rightarrow e$  in LBL accel. and atmospheric expts

$\mu \rightarrow \tau$  ( $\Delta m^2, \theta_{23}$ )



# Sketchy 3v picture (with 1-digit accuracy)

## Knowns:

$$\begin{aligned}\delta m^2 &\sim 7 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02\end{aligned}$$



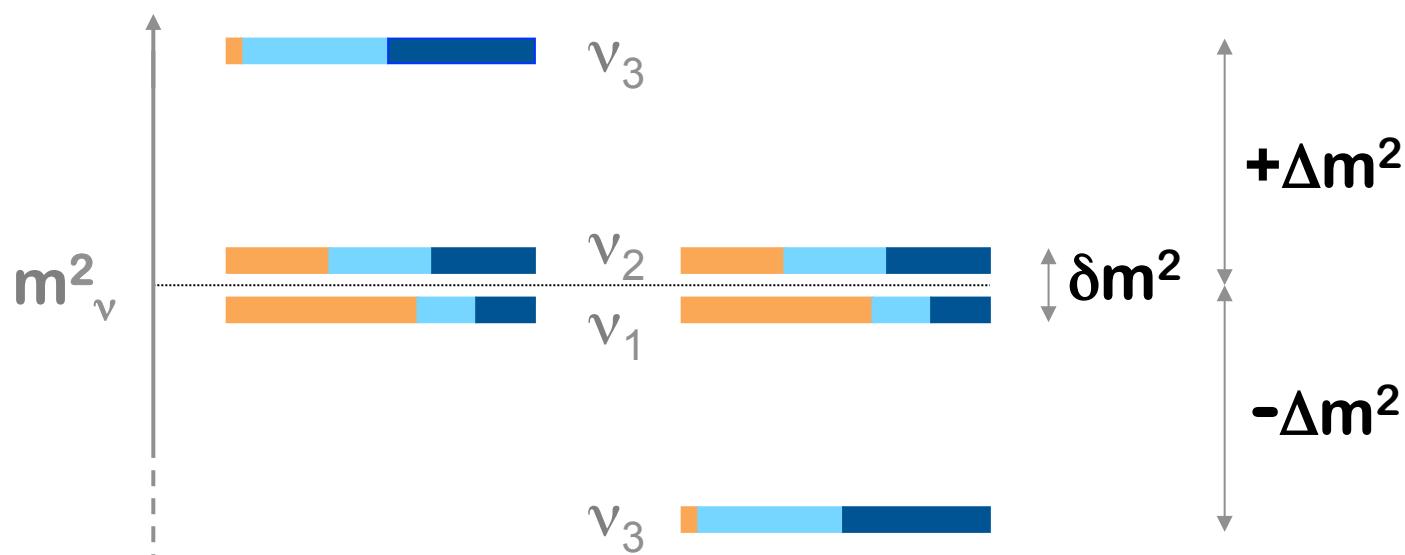
## Unknowns:

$\delta$  = Dirac CPV phase  
 $\text{sign}(\Delta m^2)$  = ordering  
octant( $\theta_{23}$ )  
absolute mass scale  
Dirac/Majorana nature

Normal Ordering (NO)

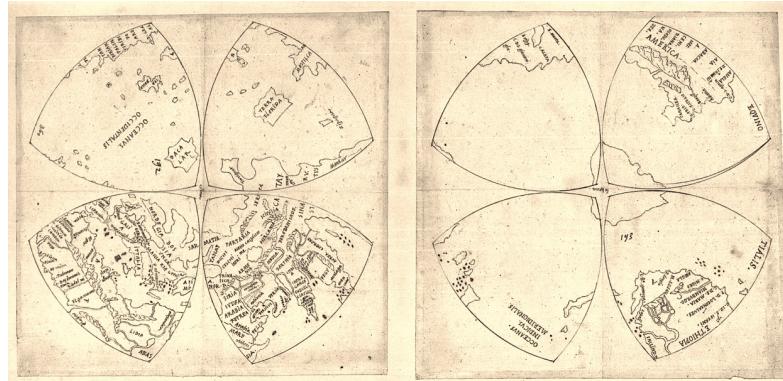
e  $\mu$   $\tau$

Inverted Ordering (IO)





**from sketch  
to full map →  
combine info  
from all v data  
“global analysis”**



Global 3v analysis: mainly based on work in collaboration with  
F. Capozzi, E. Di Valentino, A. Marrone, A. Melchiorri, A. Palazzo;  
**hep-ph 2003.08511 (PRD 101, 2020) + work in progress (2021)**

- charting the newly discovered territories →

For experts: Results of 2003.08511 are here updated with oscill. data from Neutrino 2020 (SK solar, T2K, NOvA, RENO). Still working on inclusion of latest SK-IV atmos. Non-oscillation data are the same as in 2003.08511 in this Colloquium.

# Methodology

Useful to analyze oscillation data in the following sequence:

**LBL Accel + Solar + KL** (KamLAND)

minimal set sensitive to all osc. param.:  $\delta m^2$ ,  $\Delta m^2$ ,  $\theta_{13}$ ,  $\theta_{23}$ ,  $\theta_{12}$ ,  $\delta$ , NO/IO

**LBL Accel + Solar + KL + SBL Reactor**

add sensitivity to  $\Delta m^2$ ,  $\theta_{13}$  and affect **other parameters** via correlations

**LBL Accel + Solar + KL + SBL Reactor + Atmosph.**

add sensitivity to  $\Delta m^2$ ,  $\theta_{23}$ ,  $\delta$ , NO/IO (but: entangled information in atmos.)

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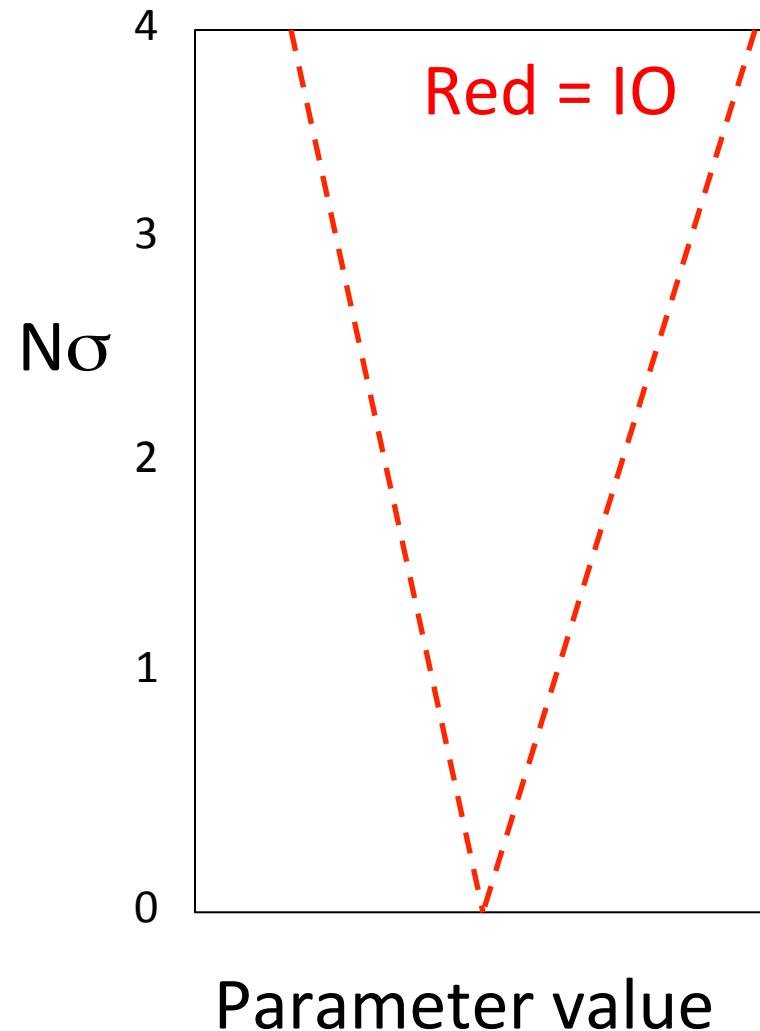
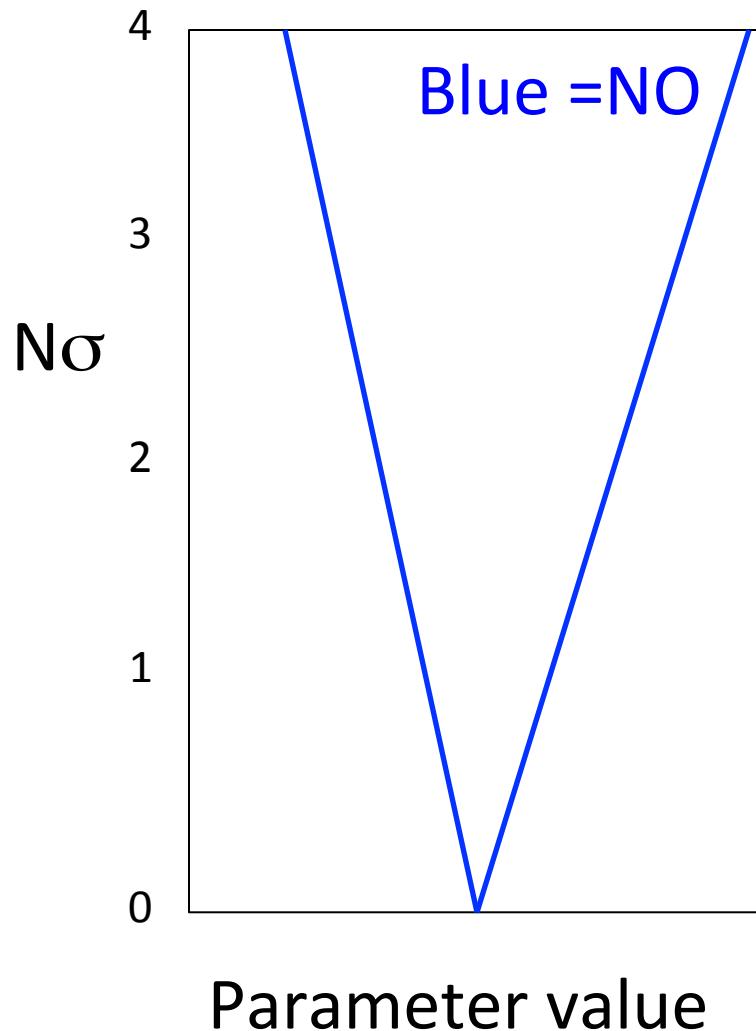
## Statistics

Bounds/contours in terms of  $N\sigma$  around best fit:  $N\sigma = \sqrt{\Delta\chi^2} = 1, 2, 3\dots$

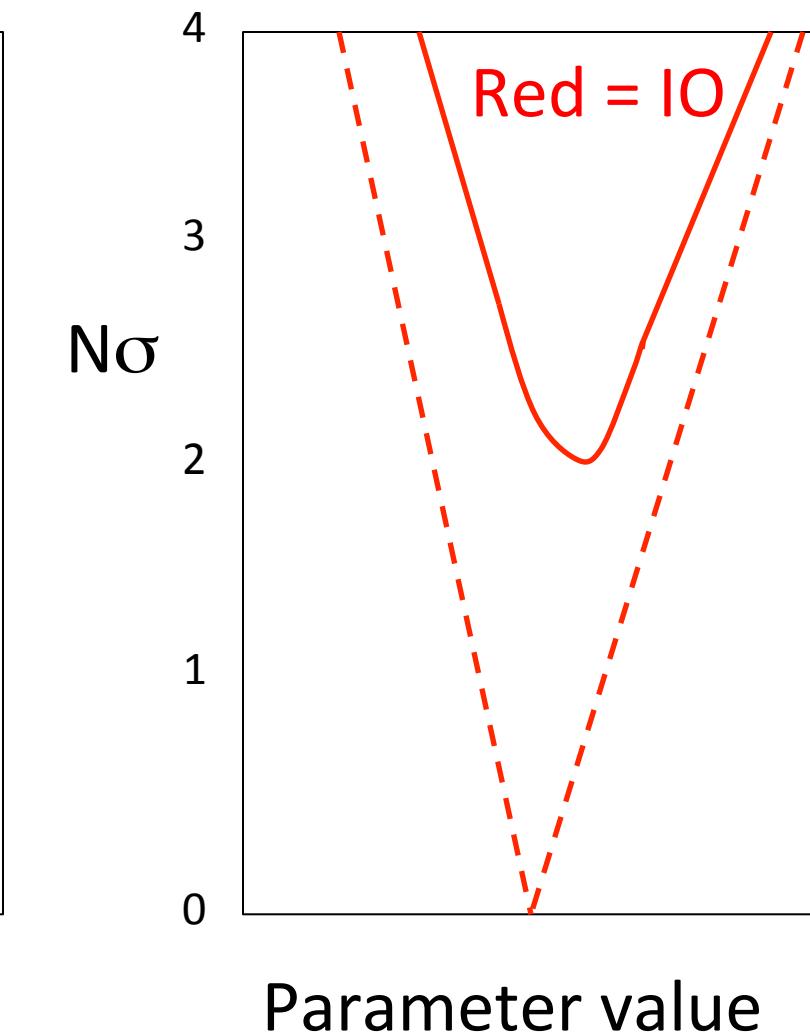
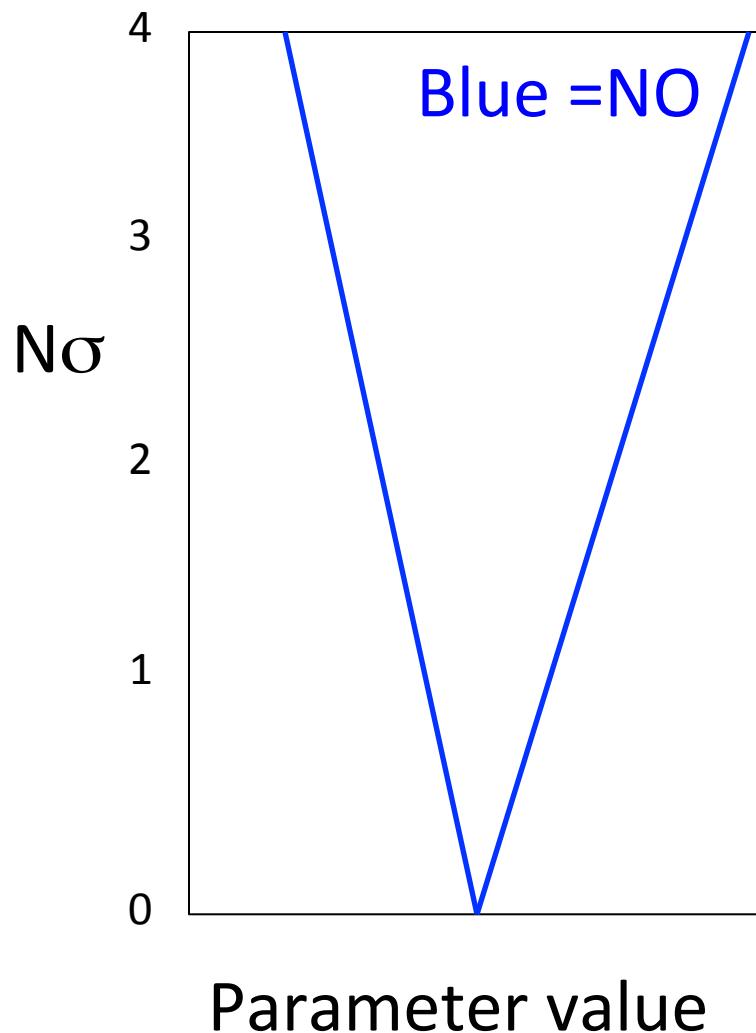
Undisplayed parameters are marginalized (projected) away

We shall discuss first “**single**” parameters and then “**pairs**” of parameters.

Single-parameter bounds would scale linearly (and symmetrically)  
in the limit of  $\sim$  gaussian errors around best fit values.

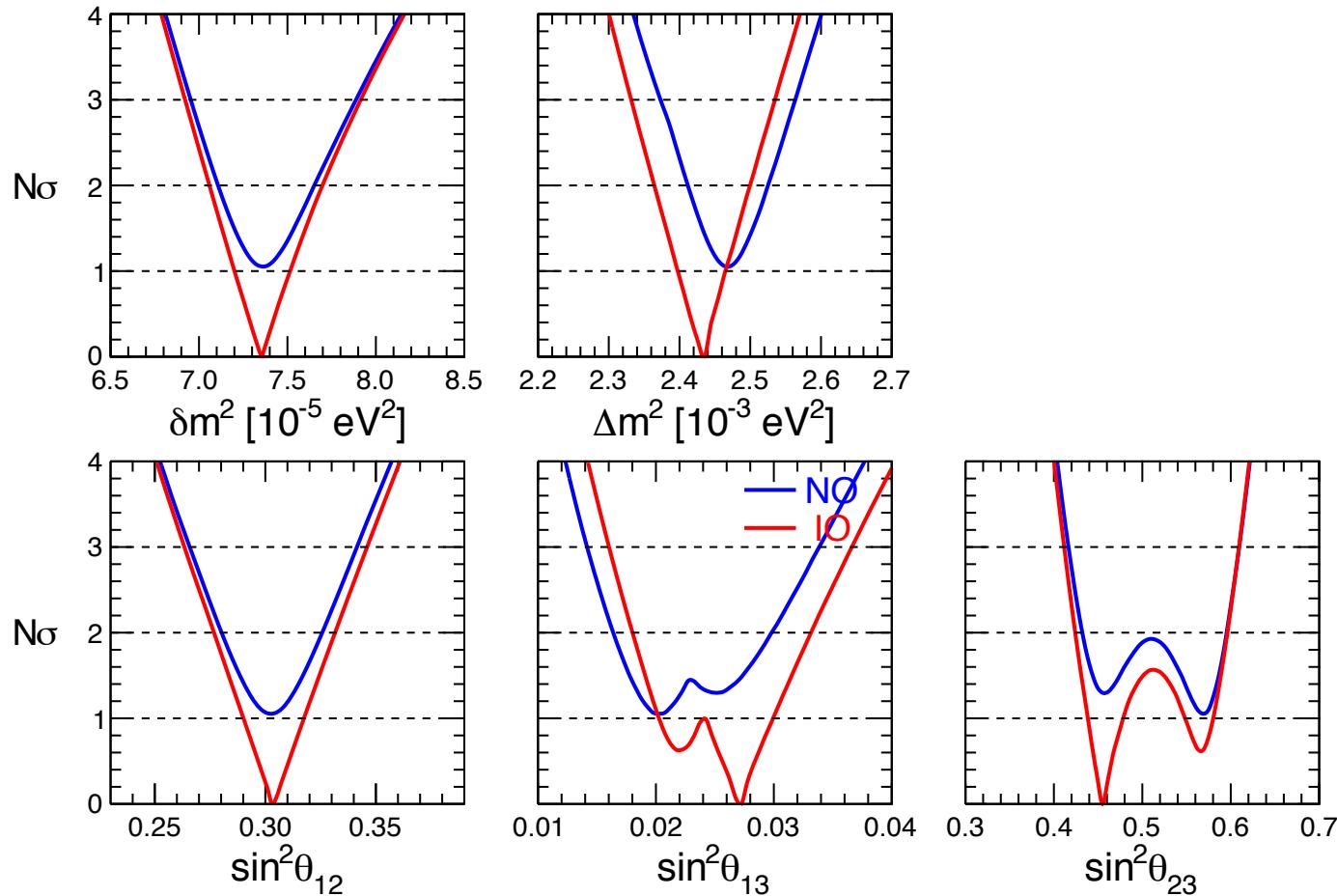


However, bounds for one given mass ordering move upwards,  
if the other mass ordering is preferred, e.g.:



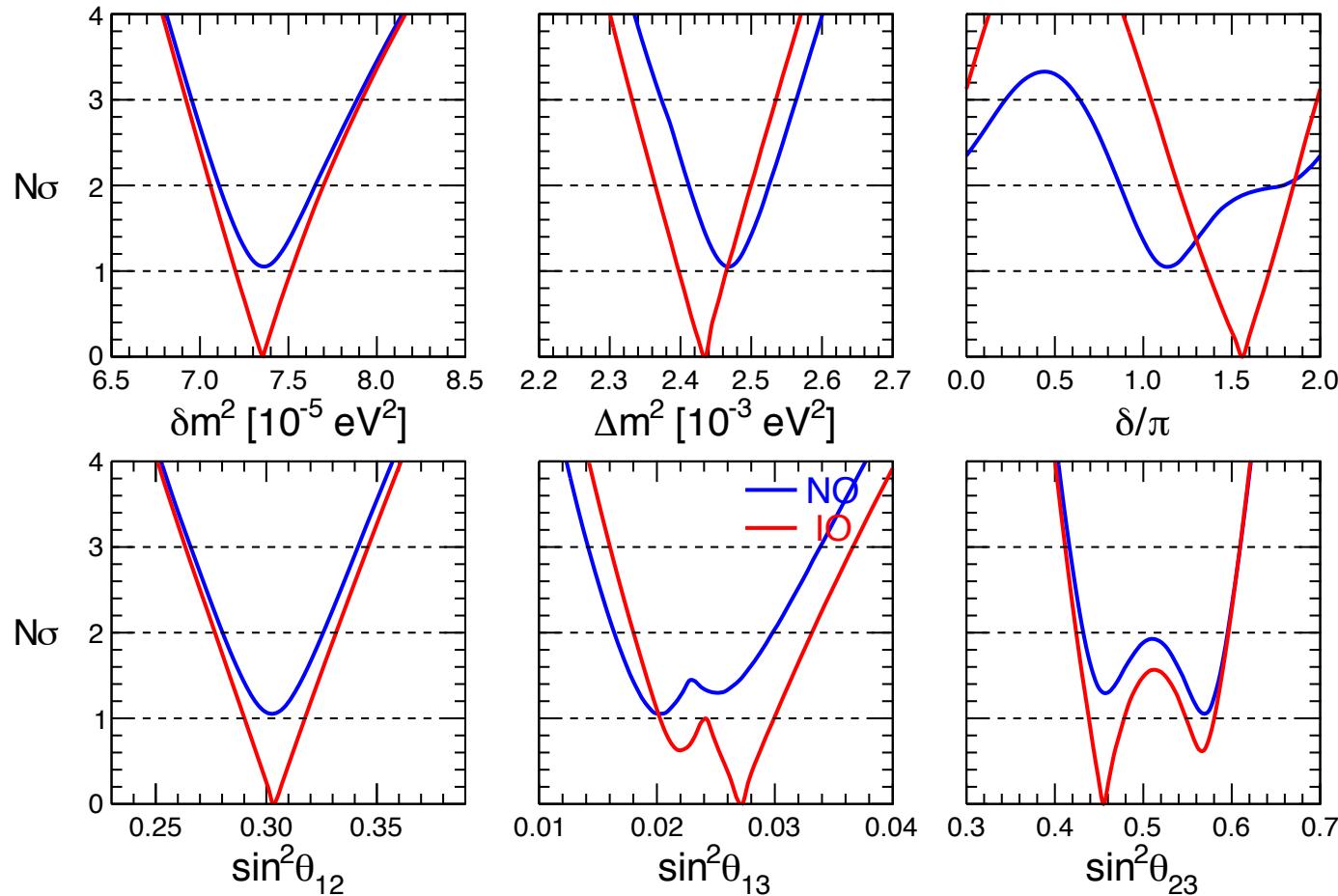
Results →

### LBL Acc + Solar + KamLAND



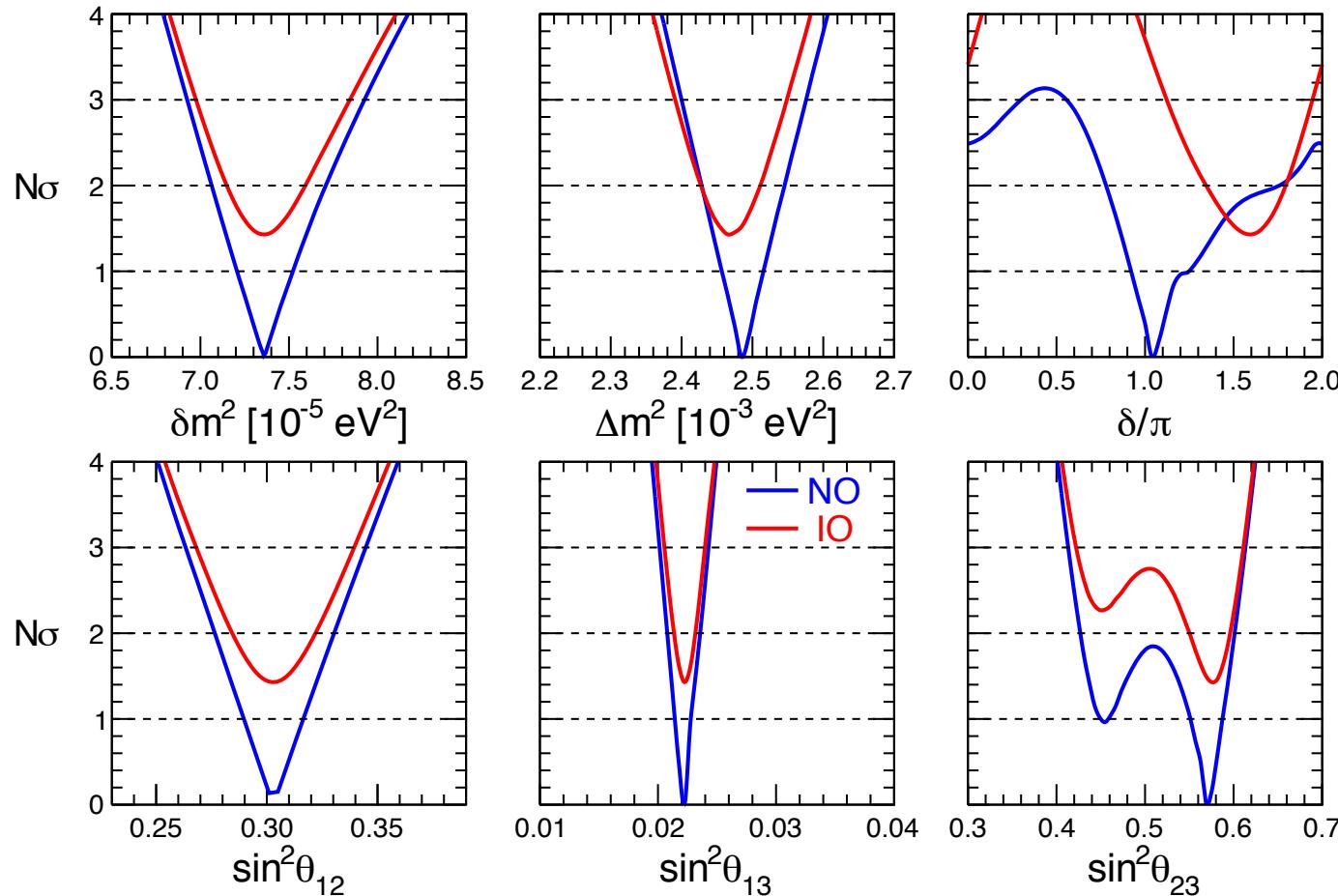
- Upper and lower bounds at  $>>3\sigma$  for  $\delta m^2$ ,  $\Delta m^2$ ,  $\theta_{12}$ ,  $\theta_{13}$ ,  $\theta_{23}$
- Weak preference for **IO** at  $\sim 1\sigma$ . Note different  $\Delta m^2$  in NO/IO
- Octant degeneracy of  $\theta_{23}$  also affects  $\theta_{13}$  via correlations in  $\nu_\mu \rightarrow \nu_e$

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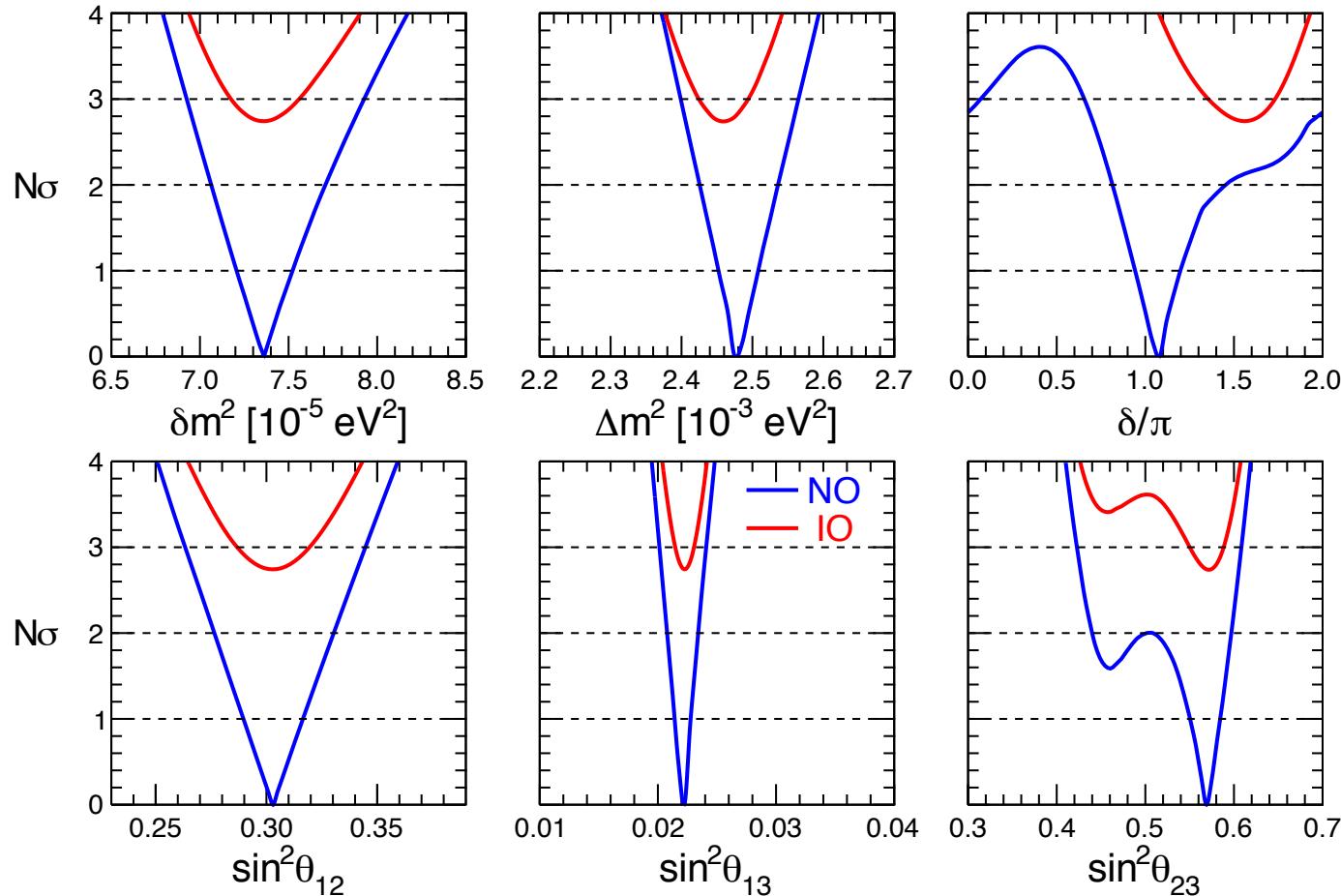
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- Octant degeneracy of  $\theta_{23}$  also affects  $\theta_{13}$  via correlations in  $\nu_\mu \rightarrow \nu_e$
- Preference for  $\delta \sim 3\pi/2$  (CP violation) in **IO**, but not in NO

### LBL Acc + Solar + KamLAND + SBL Reactors



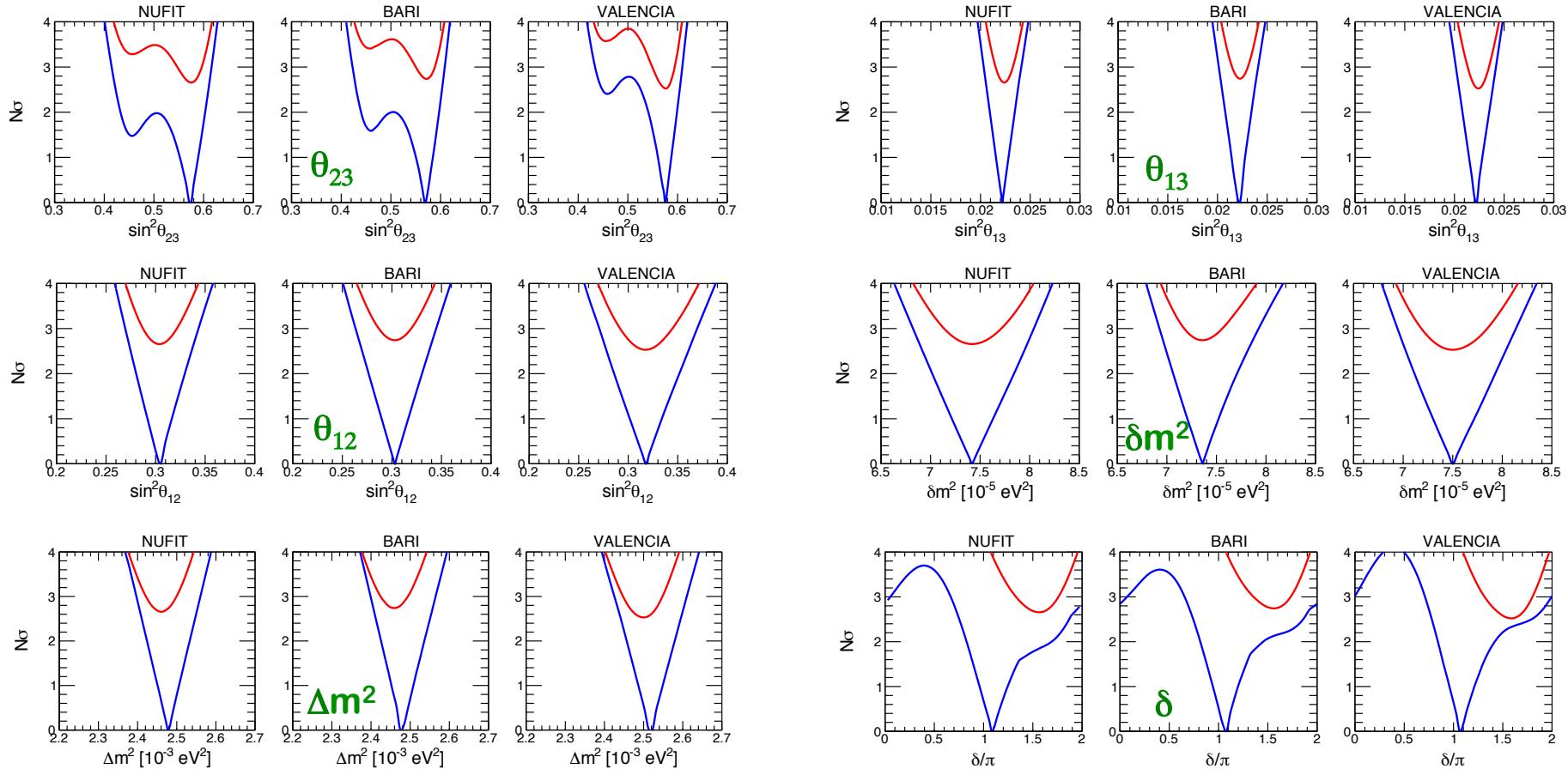
- Bounds on  $\theta_{13}$  and  $\Delta m^2$  strengthened
- Preference for **NO** at  $\sim 1.5\sigma$ . Note overall higher  $\Delta m^2$  in both NO and IO
- Octant degeneracy of  $\theta_{23}$  weakly broken, **2<sup>nd</sup> octant** preferred at  $\sim 1\sigma$
- Preference for  $\delta \sim \pi$  (CP conservation) in **NO**, while  $\delta \sim 3\pi/2$  in IO

### LBL Acc + Solar + KamLAND + SBL Reactors + Atmos



- Increased preference for **NO** ( $2.7\sigma$ )
- Increased preference for **2<sup>nd</sup> octant of  $\theta_{23}$**  ( $1.6\sigma$ )
- CP phase: best fits still around  $\delta \sim \pi$  in **NO** and  $\delta \sim 3\pi/2$  in **IO**

# Comparison among independent global neutrino oscillation data analyses



**BARI:**

2003.08511 [updated for this Colloquium]

**NUFIT:**

2007.19742 [with  $\Delta m^2_{13}$  and  $\Delta m^2_{23}$  converted to our  $\Delta m^2$ ]

**VALENCIA:**

2006.11237v2 [with  $\Delta m^2_{13}$  and  $\Delta m^2_{23}$  converted to our  $\Delta m^2$ ]

# Precision $3\nu$ cartography: Five parameters known at (few)% level

TABLE I: Updated for this Colloquium from Capozzi+ arXiv:2003.08511 [hep-ph]

Global  $3\nu$  analysis of oscillation data, in terms of best-fit values and allowed ranges at  $N_\sigma = 1, 2, 3$  for the mass-mixing parameters, in either NO or IO. The last column shows the formal “ $1\sigma$  accuracy” for each parameter, defined as  $1/6$  of the  $3\sigma$  range, divided by the best-fit value (in percent). We recall that  $\Delta m^2 = m_3^2 - (m_1^2 + m_2^2)/2$  and  $\delta/\pi \in [0, 2]$  (cyclic).

Parameter	Ordering	Best fit	$1\sigma$ range	$2\sigma$ range	$3\sigma$ range	“ $1\sigma$ ” (%)
$\delta m^2/10^{-5}$ eV $^2$	NO, IO	7.36	7.21 – 7.52	7.06 – 7.71	6.93 – 7.93	2.3
$\sin^2 \theta_{12}/10^{-1}$	NO, IO	3.03	2.90 – 3.16	2.77 – 3.30	2.63 – 3.45	4.5
$ \Delta m^2 /10^{-3}$ eV $^2$	NO	2.475	2.453 – 2.508	2.426 – 2.536	2.399 – 2.565	1.1
	IO	2.455	2.431 – 2.487	2.403 – 2.516	2.374 – 2.545	1.2
$\sin^2 \theta_{13}/10^{-2}$	NO	2.23	2.15 – 2.28	2.08 – 2.34	2.01 – 2.41	3.0
	IO	2.23	2.16 – 2.29	2.10 – 2.35	2.03 – 2.42	2.9
$\sin^2 \theta_{23}/10^{-1}$	NO	5.69	5.50 – 5.84	4.40 – 5.97	4.23 – 6.08	5.4
	IO	5.69	5.54 – 5.85	5.28 – 5.98	4.25 – 6.08	5.4
$\delta/\pi$	NO	1.08	0.94 – 1.20	0.82 – 1.45	0 – 0.07 $\oplus$ 0.65 – 2	22
	IO	1.56	1.40 – 1.70	1.22 – 1.83	1.06 – 1.94	9

Most accurate parameter is  $\Delta m^2$ : “formal” uncertainty as small as  $\sim 1\%$  !  
 Q.: Is such accuracy “robust”? Any bias? More later.

# Pairs of parameters

Some relevant covariances:

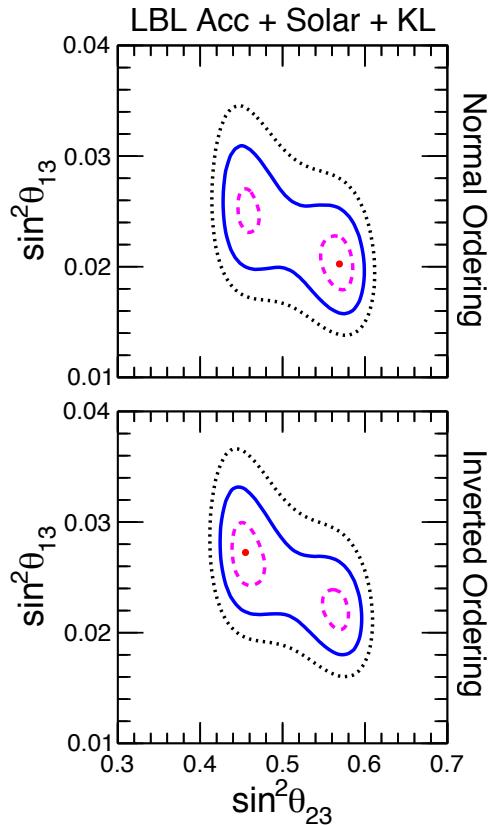
$$(\theta_{13}, \theta_{23})$$

$$(\theta_{13}, \pm\Delta m^2)$$

$$(\theta_{12}, \delta m^2)$$

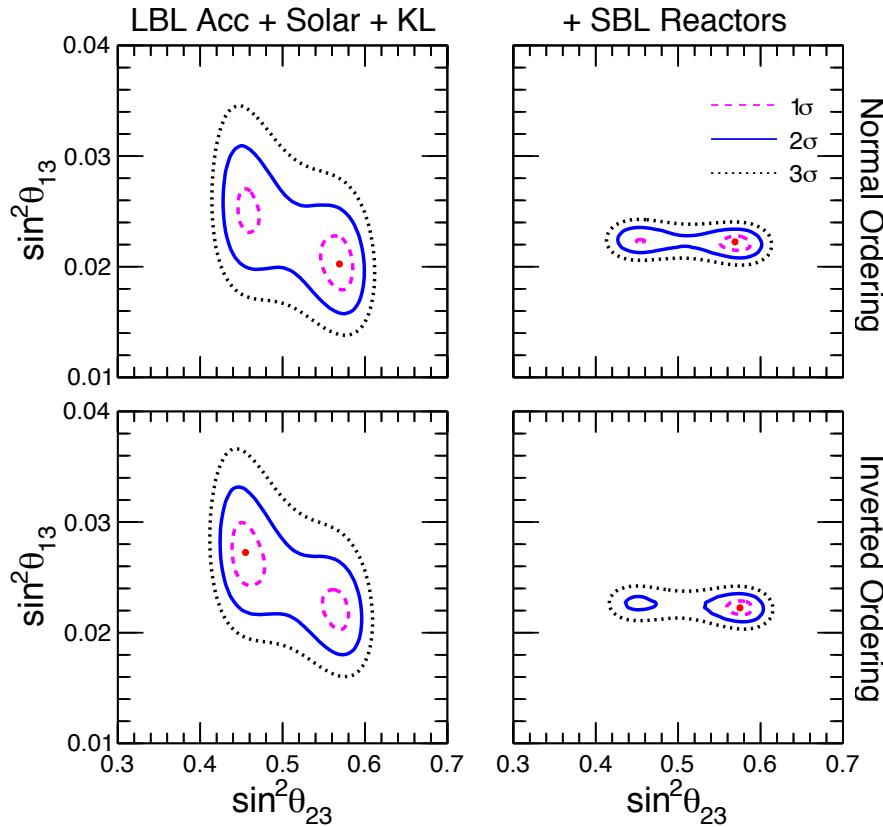


$(\theta_{13}, \theta_{23})$  covariance



Anticorrelation due to  
leading  $\nu_\mu \rightarrow \nu_e$  term  
 $\sim \sin^2 \theta_{23} \sin^2 2\theta_{13}$

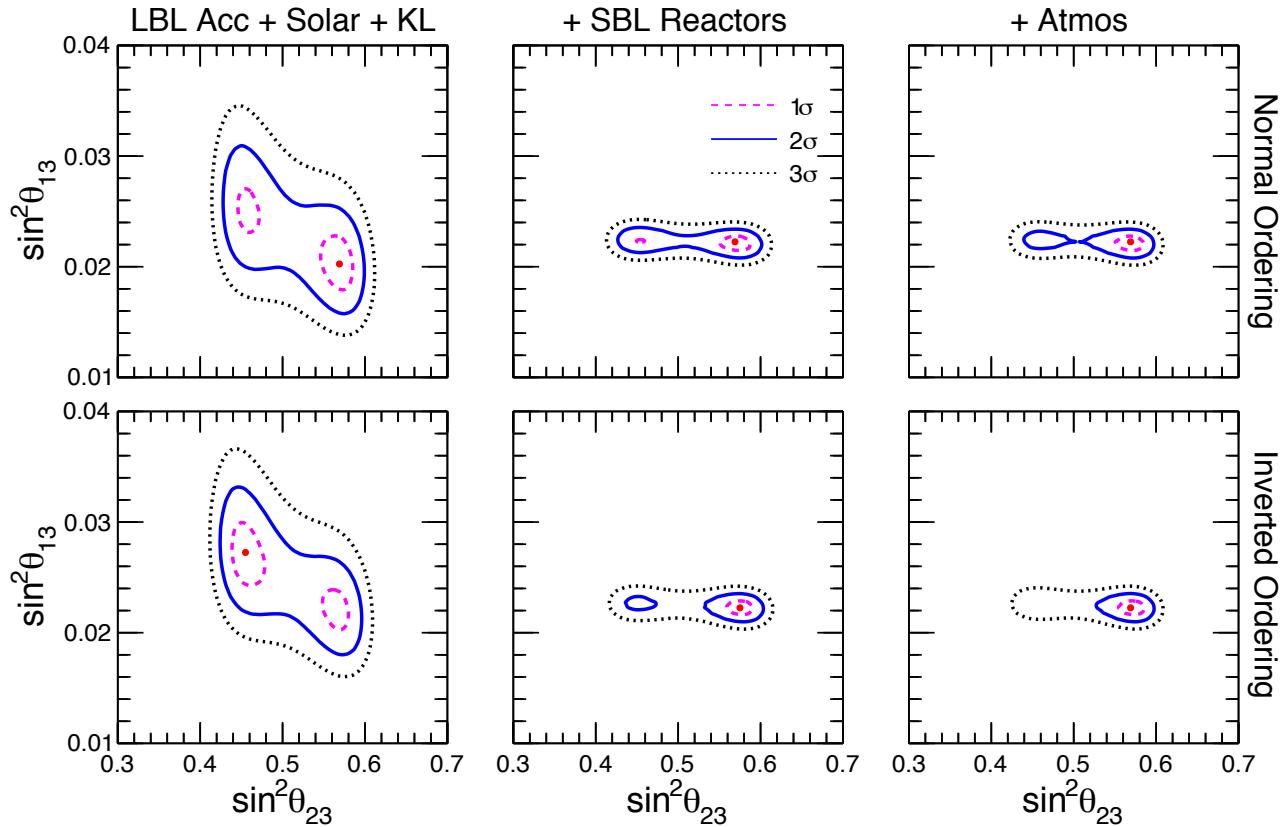
## ( $\theta_{13}$ , $\theta_{23}$ ) covariance



Anticorrelation due to  
leading  $\nu_\mu \rightarrow \nu_e$  term  
 $\sim \sin^2 \theta_{23} \sin^2 2\theta_{13}$

Narrow and “low”  $\theta_{13}$   
reactor angle  
selects 2<sup>nd</sup> octant

## ( $\theta_{13}$ , $\theta_{23}$ ) covariance

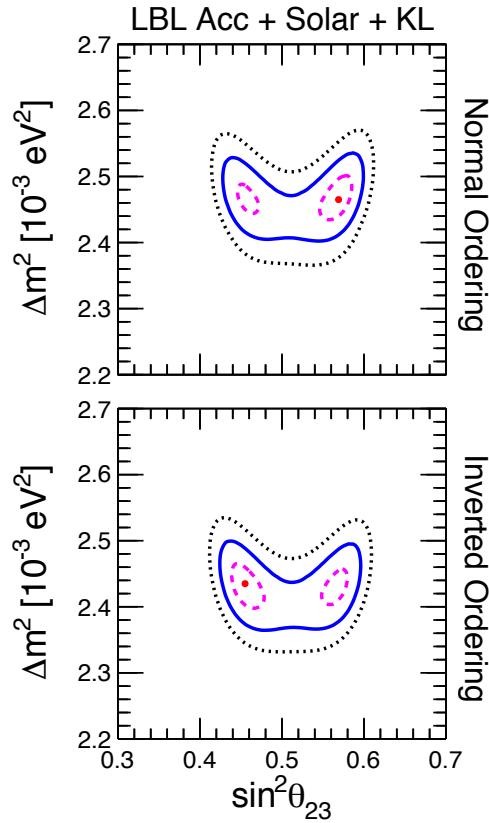


Anticorrelation due to  
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Narrow and “low”  $\theta_{13}$   
reactor angle  
selects 2<sup>nd</sup> octant

2<sup>nd</sup> octant confirmed  
by atmospheric data  
in both NO and IO  
(but: fragile!)

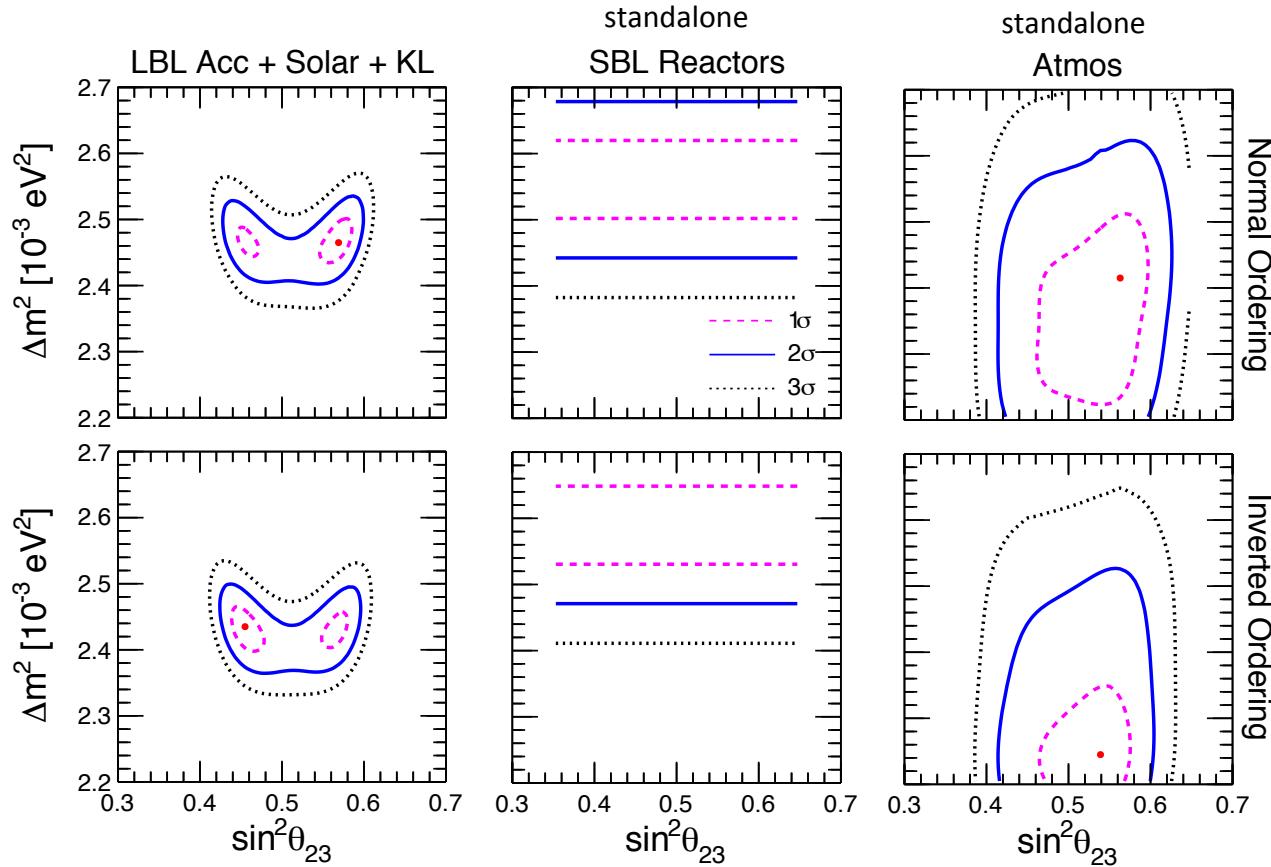
$(\theta_{23}, \pm \Delta m^2)$  covariance



LBL data: Best fit value of  $\Delta m^2$  below  $2.5 \times 10^{-3} \text{ eV}^2$ .

The higher is  $\Delta m^2$ , the more non-max is  $\theta_{23}$ . Note **octant** ambiguity.

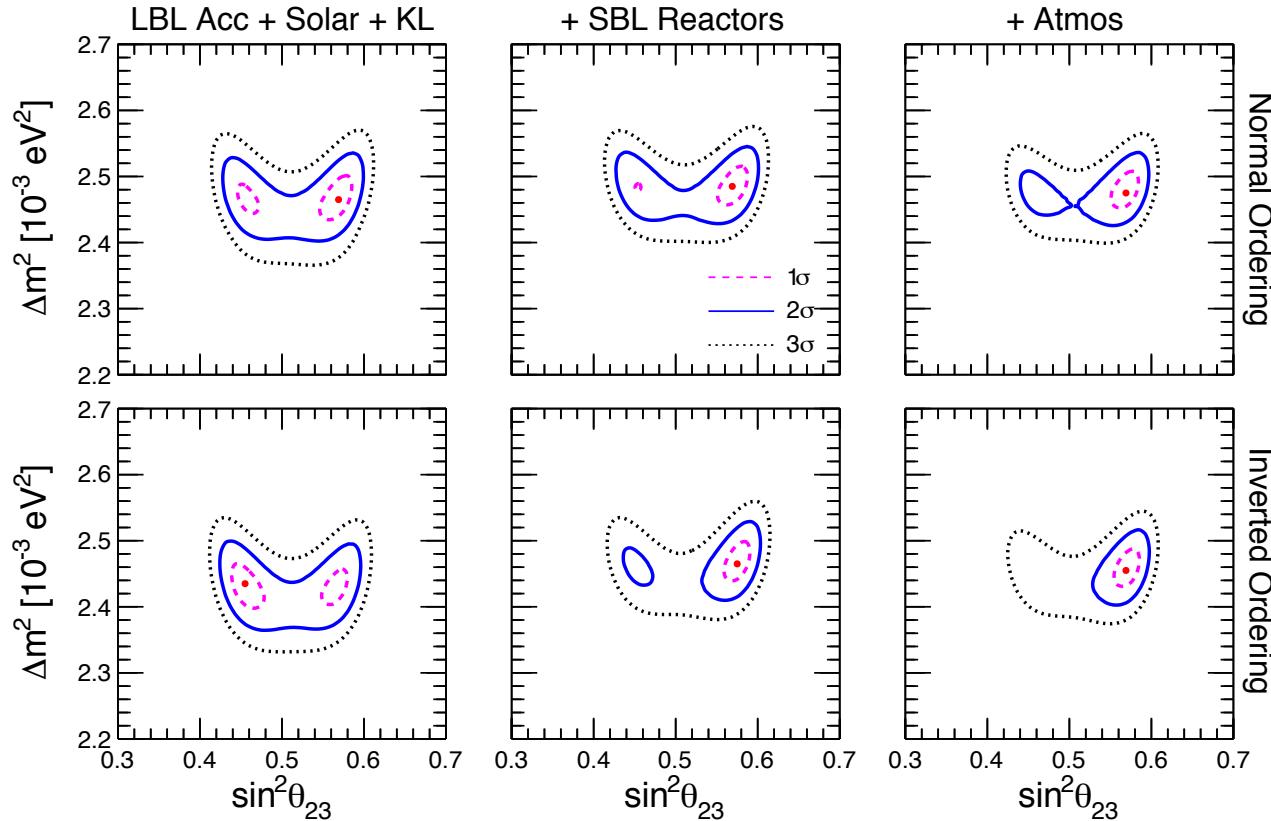
$(\theta_{23}, \Delta m^2)$  covariance



Reactors prefer higher  $\Delta m^2 (> 2.5 \times 10^{-3} \text{ eV}^2)$  than LBL accel. and atmos. exts.

Relative difference is lower for NO and for non-maximal  $\theta_{23}$  mixing

$(\theta_{23}, \Delta m^2)$  covariance



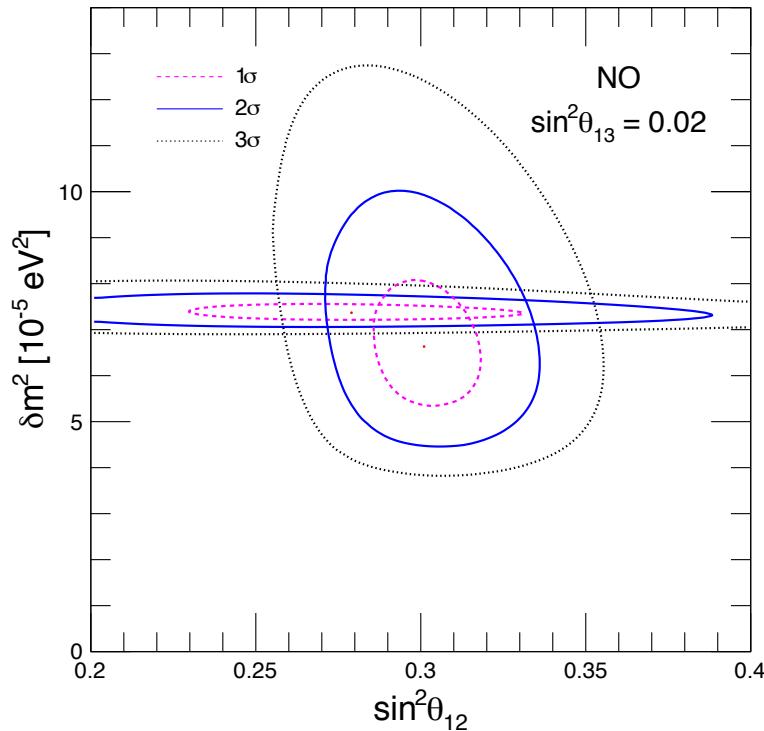
Reactors prefer higher  $\Delta m^2$  ( $> 2.5 \times 10^{-3} \text{ eV}^2$ ) than LBL accel. and atmos. exts.

Relative difference is lower for **NO** and for non-maximal  $\theta_{23}$  mixing

→ Better convergence reached for **NO**, **nonmax  $\theta_{23}$** , intermediate  $\Delta m^2$

*Accelerator/reactor complementarity at work!*

## ( $\theta_{12}$ , $\delta m^2$ ) covariance



After the latest SK solar neutrino data (Neutrino 2020), there is no longer “tension” between  $\delta m^2$  values of Solar vs KamLAND

[Tension might have pointed to new physics, like NSI, in solar neutrinos...]

- trying to avoid distortions and biases...

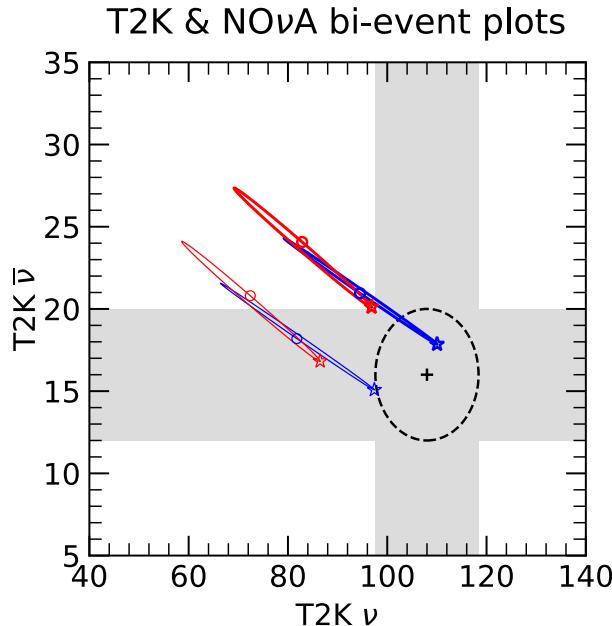
An interesting “data tension” emerges now within LBL accelerators (**T2K vs NOvA**) – whose differences in  $\nu_\mu \rightarrow \nu_e$  findings blur the (previously stronger) preference for NO and for CP violation.

→ some details for experts (bi-event plots)

Speculations on a possible role of  **$\nu$  interaction** uncertainties

→ general comments for all (EW nuclear physics)

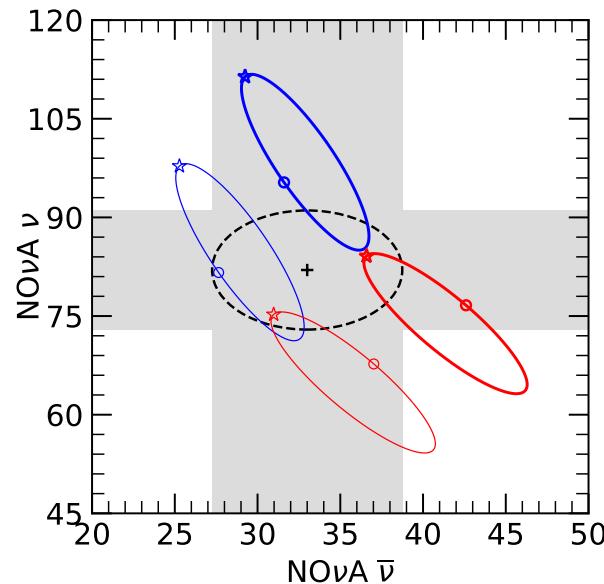
## Integrated info on $\nu$ and $\bar{\nu}$ , stat. errors only. [Not used in fits]



$$s_{23}^2 = \frac{0.57}{0.45} \quad \text{NO} \quad \text{IO} \quad \delta = \frac{\pi}{3\pi/2} \quad \star$$

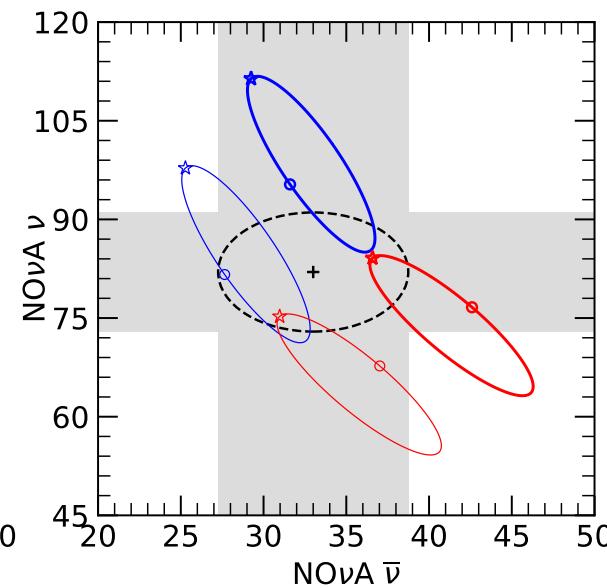
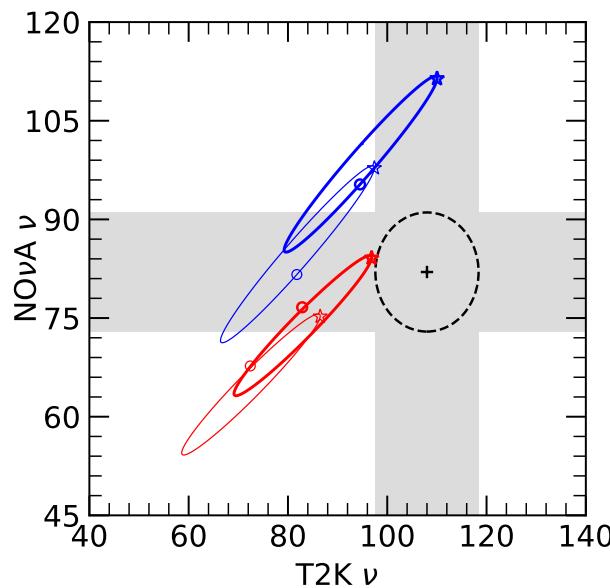
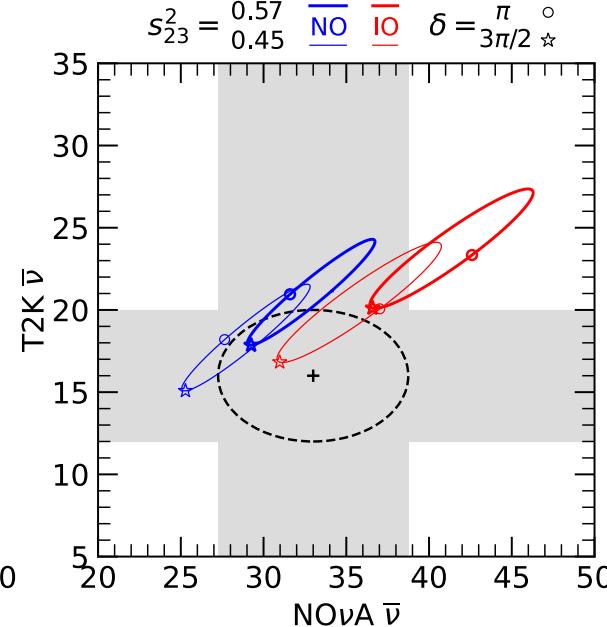
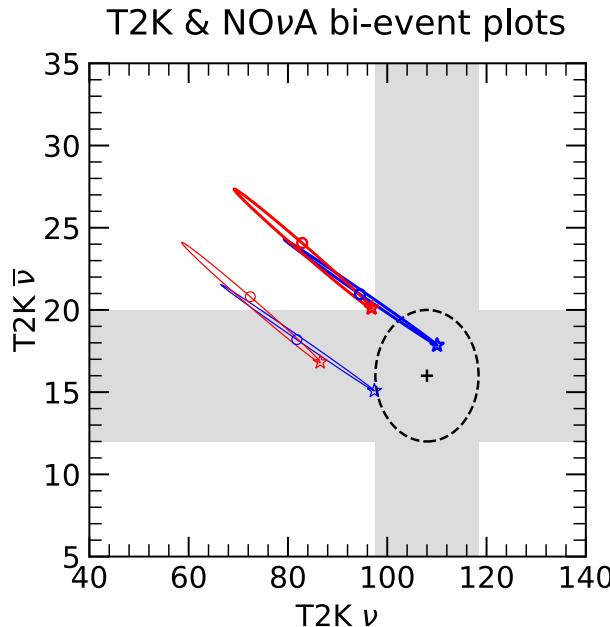
**T2K ( $\nu+\bar{\nu}$ ) prefers:**  
**NO**  
 $\delta \sim 3\pi/2$  (~max CPV)  
**2<sup>nd</sup> octant**

**NOVA ( $\nu+\bar{\nu}$ ) prefers:**  
**NO**  
**CP conservation**  
**octants ~degenerate**



→ T2K and NOVA, separately: **NO preferred; CP and octant ambiguous**

## The same info can be reorganized in terms of T2K vs NO $\nu$ A:



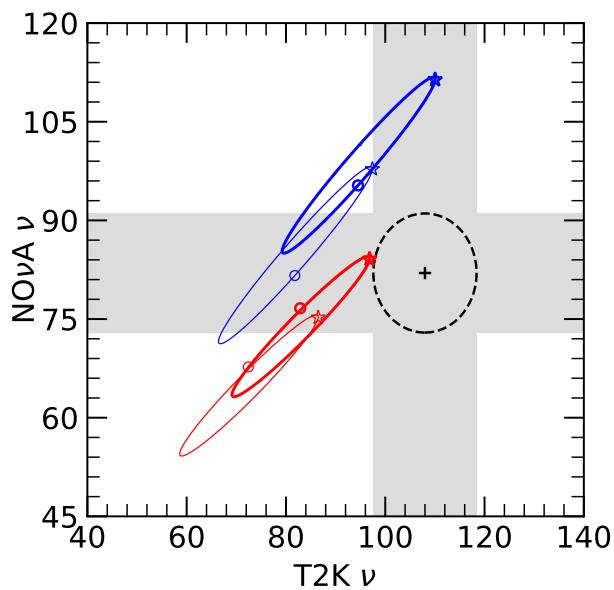
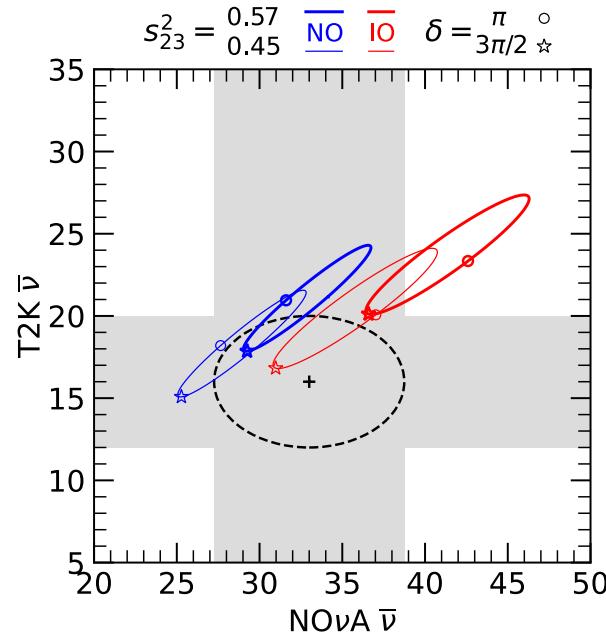
## T2K & NO $\nu$ A bi-event plots

**T2K+NO $\nu$ A ( $\nu$ ) prefer:**

**IO**

$\delta \sim 3\pi/2$

1<sup>st</sup> octant



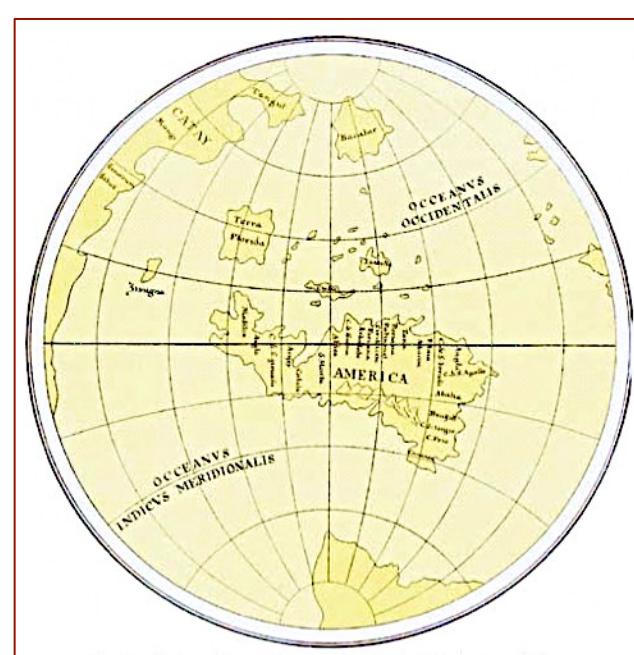
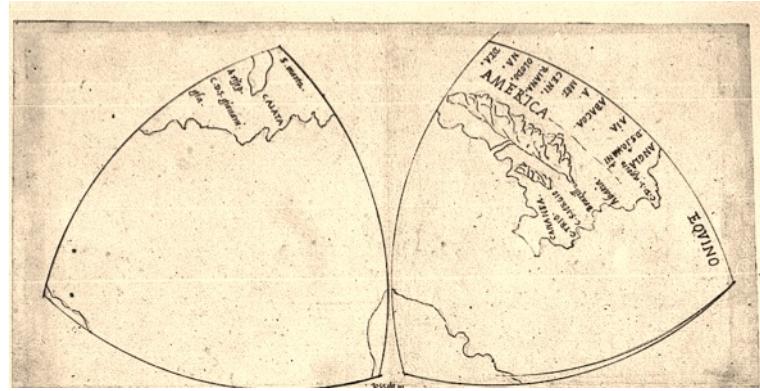
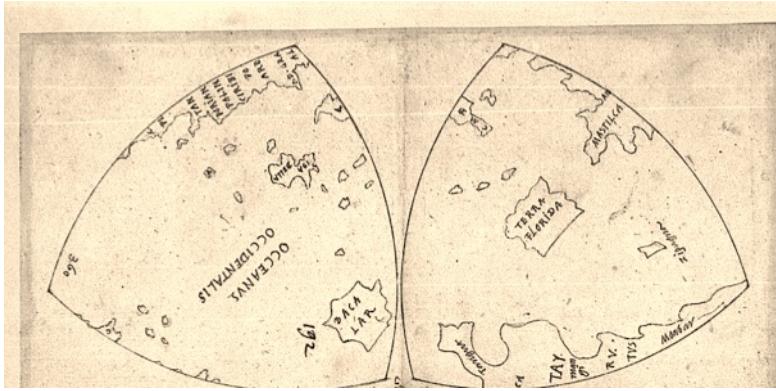
**T2K+NO $\nu$ A ( $\bar{\nu}$ ) prefer:**

**IO**

$\delta \sim 3\pi/2$

2<sup>nd</sup> octant

→ T2K and NOVA, jointly: **IO and CPV preferred; octant ambiguous**

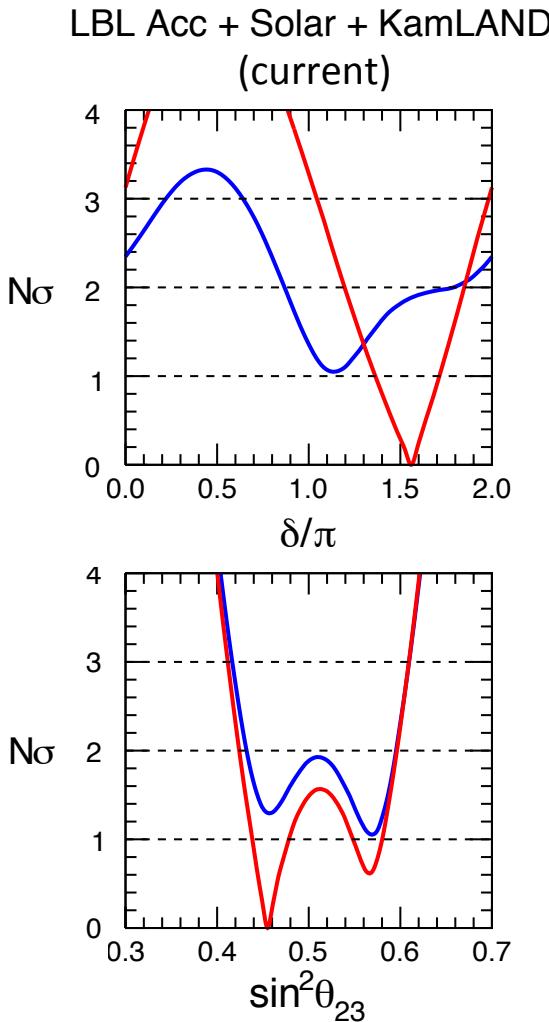


Not yet a convincing transition from “unknown” to “known” lands...

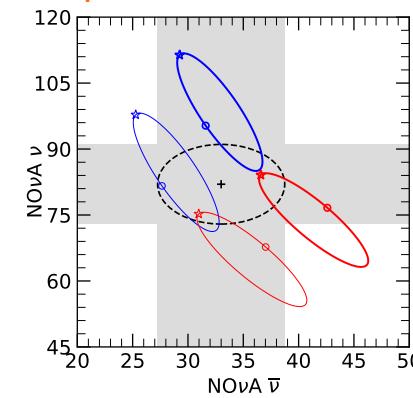
...In the T2K+NOvA combination, still unstable results on three unknowns:

**mass ordering (NO vs IO),  $\theta_{23}$  octant and CP phase  $\delta$**

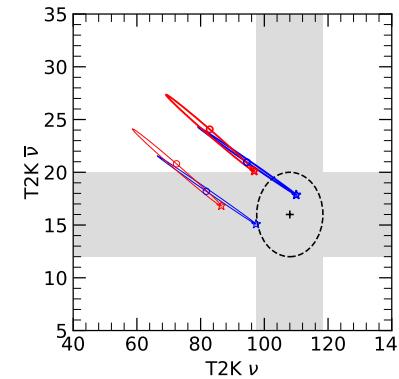
**Further data may tilt the current balance...**



**NOvA close to different options within  $1\sigma$ ...**

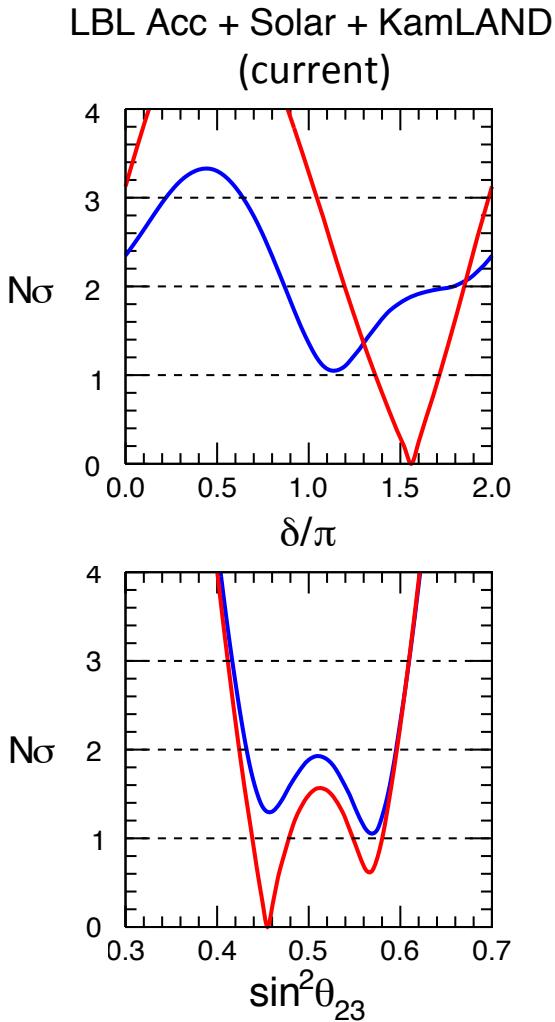


**T2K close to the edge of expected Asimov sensitivity...**

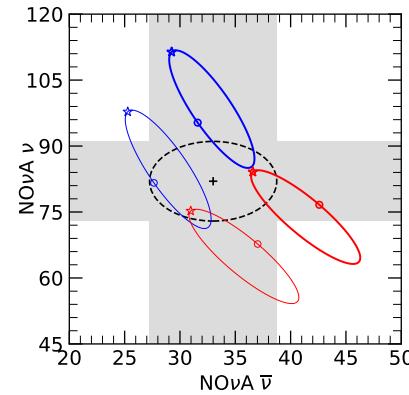


We'll learn a lot more from current LBL accel. (T2K+NOvA) + atmos. expts (SK, IC-DC), final SBL reactor data (DYB, RENO, DC), and future experiments (DUNE, HK, T2HK, IC-lowE upgrade, KM3NeT-Orca, JUNO ...). In the meantime:

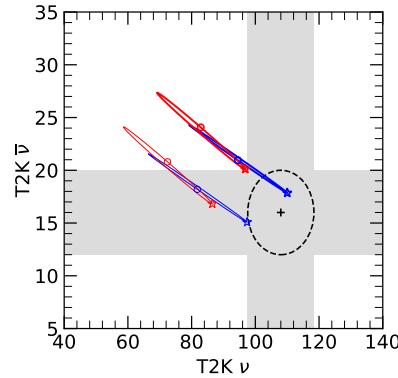
## Q.: Is there only statistics behind the T2K/NOvA tension?



NOvA close to different options within  $1\sigma$ ...

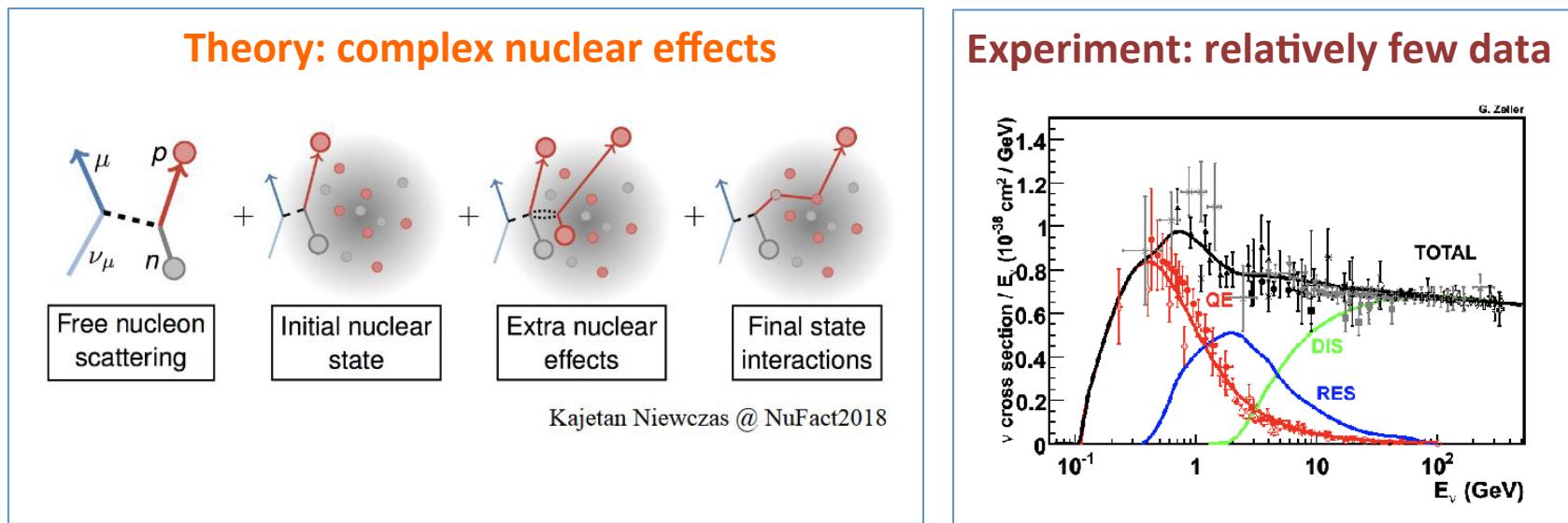


T2K close to the edge of expected Asimov sensitivity...



Parameter covariances and data tensions show the delicate interplay between 2 knowns [ $\Delta m^2$ ,  $\theta_{23}$ ] and 3 unknowns [NO/IO,  $\delta$ , sign ( $\theta_{23} - \pi/4$ )]

There is a general issue that affects all these (un)knowns:  
**neutrino interactions in nuclei are not understood as accurately as desired!**



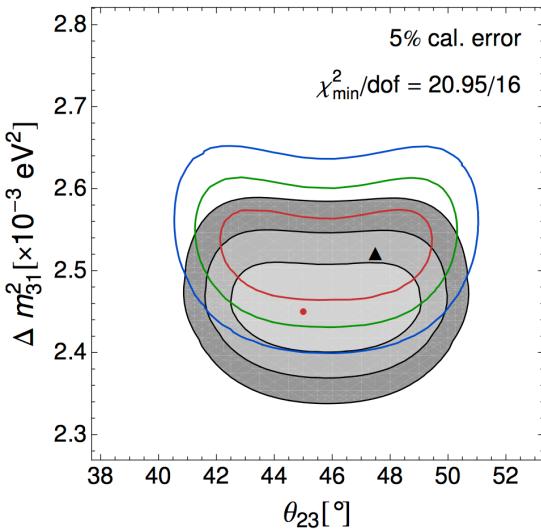
Great effort to improve the situation through dedicated experiments (including near detectors, ND) and improved nuclear models (including tuning to the above experiments), but non-negligible uncertainties remain.

# Neutrino-nuclear interactions and LBL accelerator experiments

Cross section uncertainties may affect:  
 $\Delta m^2$  (via  $E_{\text{rec}}$ ),  $\theta_{23}$  (via spectral norm+shape),  $\delta$  (via  $\nu-\bar{\nu}$  interaction differences)

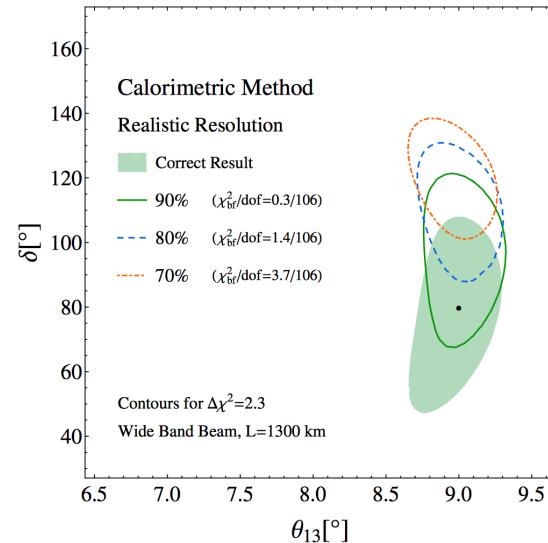
Exercise to estimate bias:

Generate data with one Xsec model and analyze them with a different model



← Biased →  
ranges of  
 $\Delta m^2, \theta_{23}$   
 $\delta$

[Benhar+ 1501.06448,  
Alvarez+ 1706.03621,  
and refs. therein]



Effects reduced -but not zeroed- by tuning model(s) to ND data.  
Remind: No model currently explains all available Xsection data!  
Current 1% global-fit formal accuracy on  $\Delta m^2$  might be optimistic

But... there is much more than just cross sections for HEP!

Beta decays for nuclear reactor spectra

Coherent Elastic Neutrino  
Nucleus Scattering

Charge exchange processes for DBD NME

Neutrinos in very dense fermion  
backgrounds (SN, early universe)

Effective neutrino axial current:  
coupling strength and form factors

Nuclear astrophysics and neutrinos  
(nucleosynthesis & solar reactions networks)

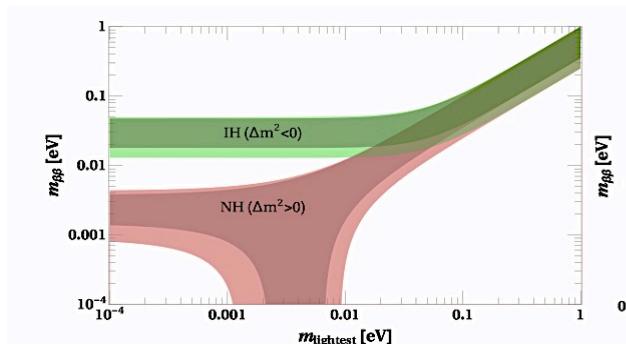
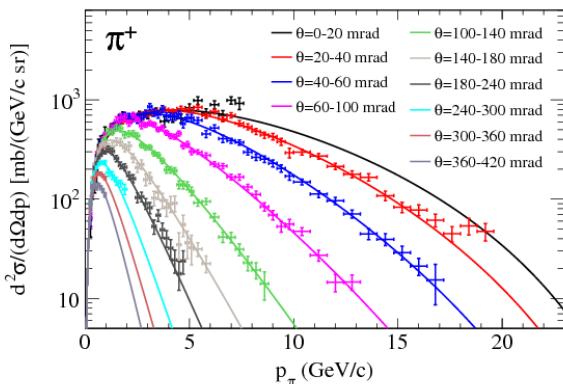
EFT vs QCD

Ab initio nuclear structure

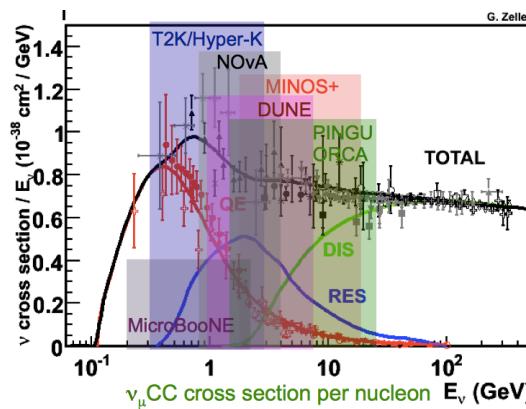
EC processes and neutrino mass  
Connections with other EW probes  
(gammas, electron, possible WIMPs...)

# “Strong interaction” effects on “weak interaction” physics are ubiquitous...

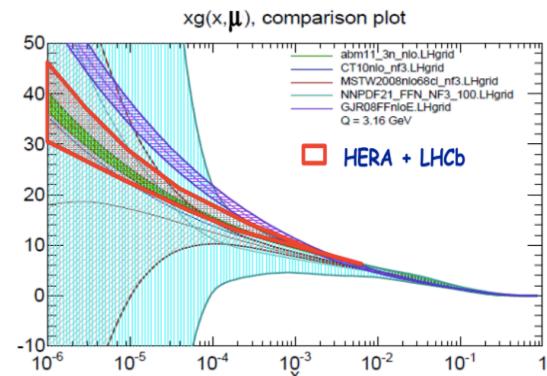
Need hadron production data, e.g.  $pA \rightarrow \pi X$ , +theory models to improve estimates of atm. and acceler.  $\nu$  fluxes and errors



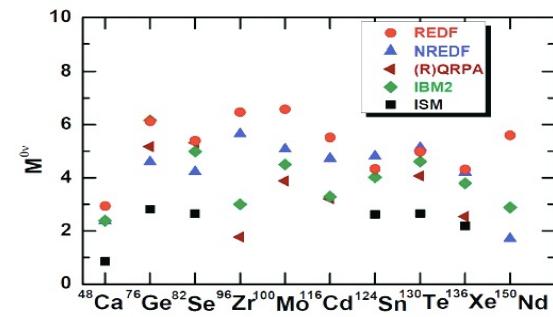
Current understanding of  $\nu$  cross sections at  $O(\text{GeV})$  does not match the needs of (next-generation)  $\nu$  expts



Improved PDFs at low- $x$  via ~forward charm production at LHCb essential to constrain prompt component in UHE  $\nu$



Better control of nuclear EW response (e.g.,  $g_A$ ) relevant to interpret  $2\beta$  data and to connect them with other data, including reactor spectra...

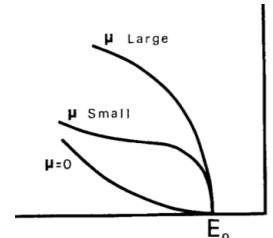


Progress requires joint contributions from different disciplines & communities:  
→ emerging field of “Electroweak Nuclear Physics”; needs support!

# Absolute neutrino mass and Dirac/Majorana nature: The last 3ν unknowns & their observables ( $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ )

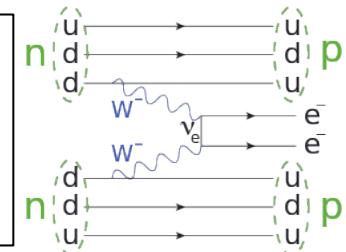
**β decay**, sensitive to the “effective electron neutrino mass”:

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$



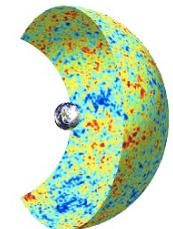
**0νββ decay**: only if Majorana. “Effective Majorana mass”:

$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$



**Cosmology**: Dominantly sensitive to sum of neutrino masses:

$$\Sigma = m_1 + m_2 + m_3$$

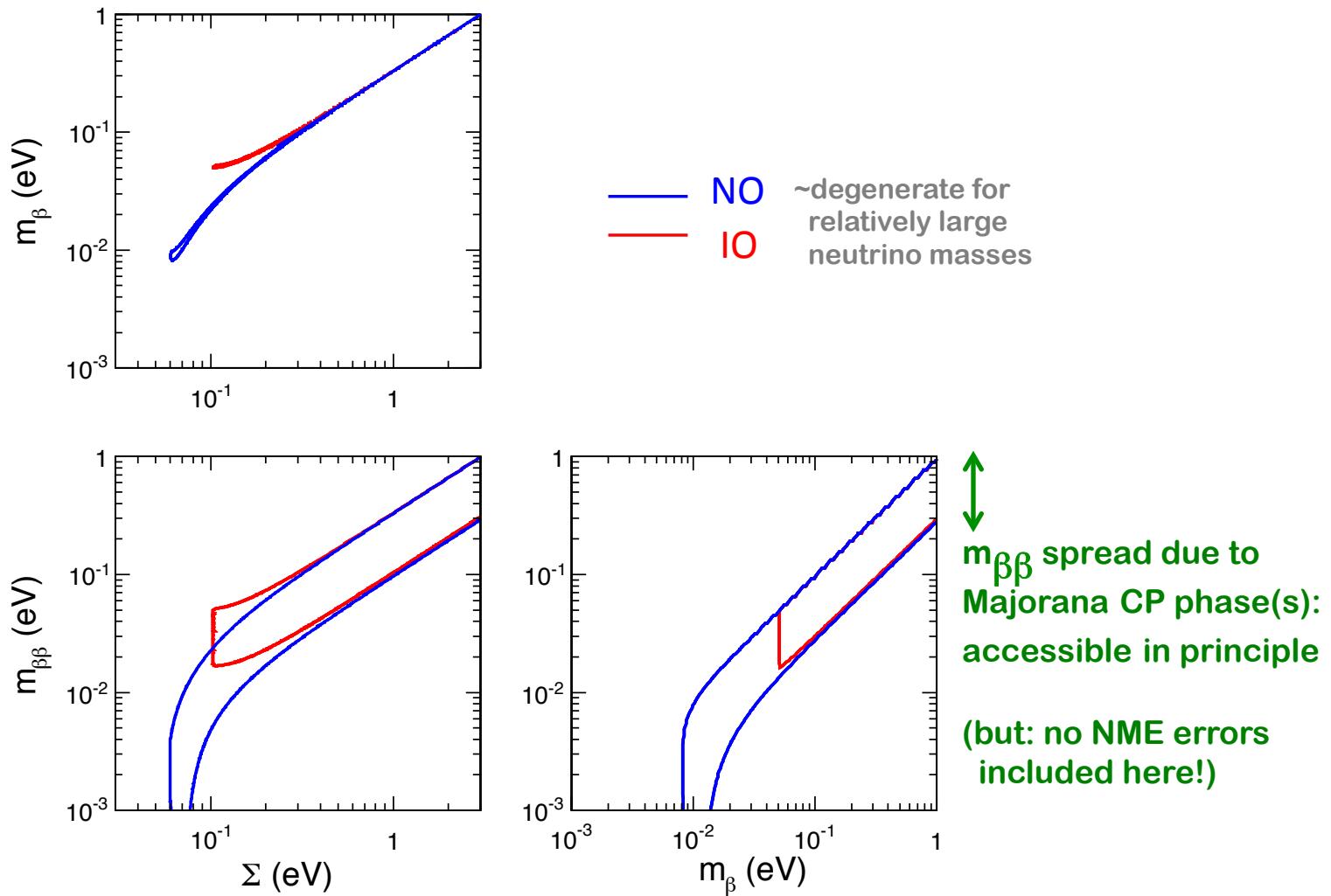


Note 1: These observables may provide handles to distinguish NO/IO.

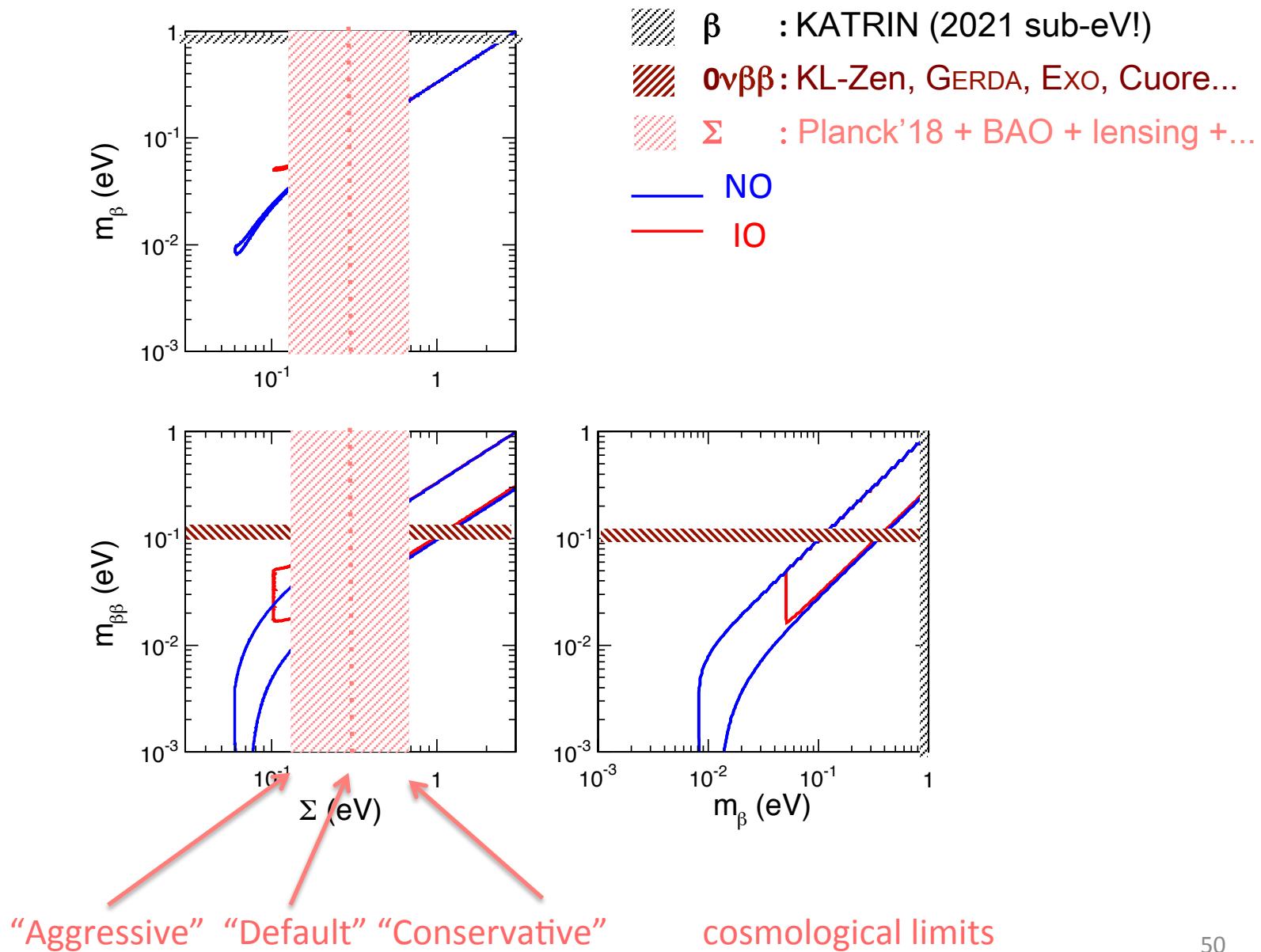
Note 2: Majorana case gives a new source of CPV (unconstrained)

**Note 2: The three observables are correlated by oscillation data →**

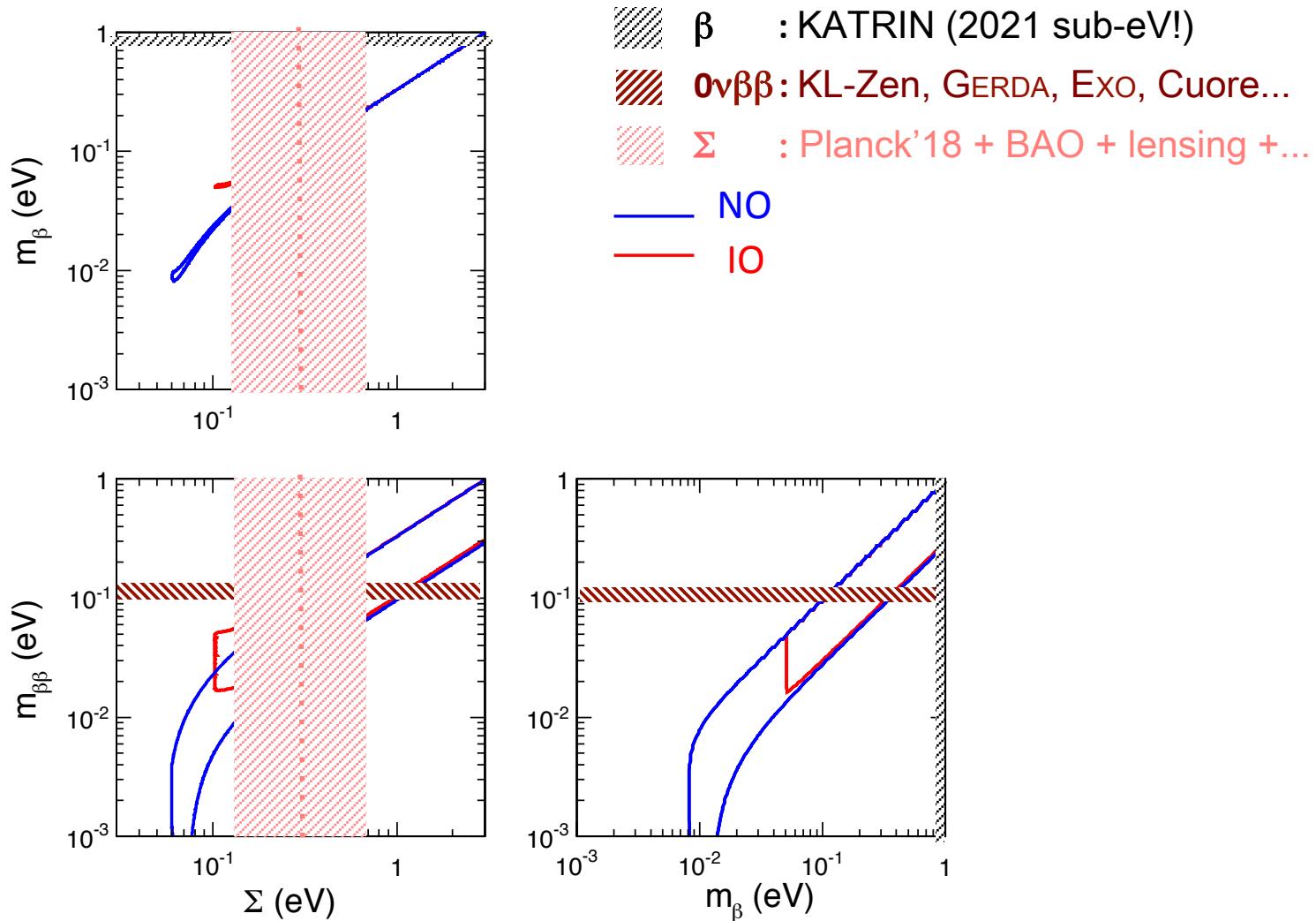
# Impact of oscillations on non-oscillation parameter space



# No signal (yet), but upper limits on $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ (up to some syst.)



# No signal (yet), but upper limits on $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ (up to some syst.)

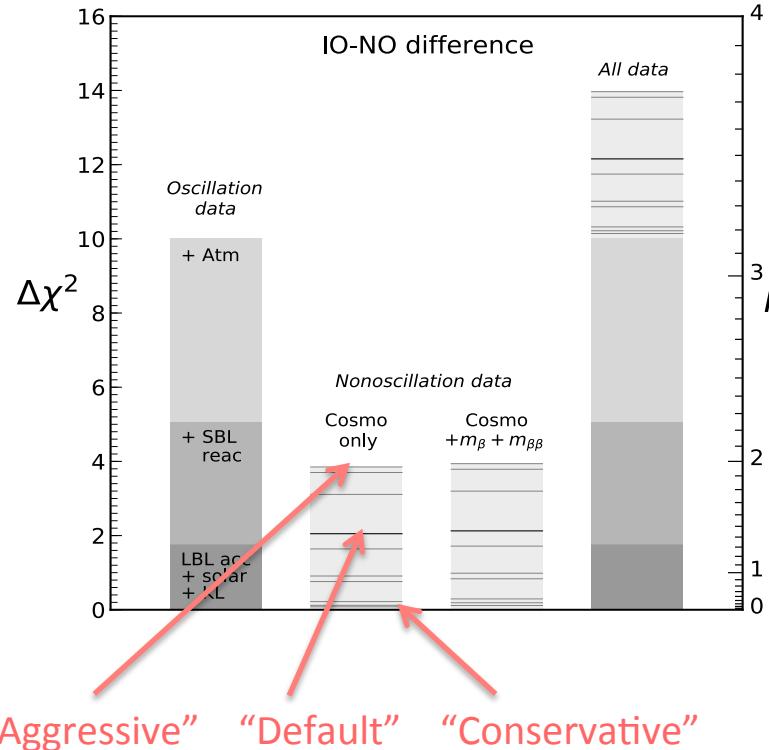


Cosmo data constrain masses and generally put IO “under pressure” →

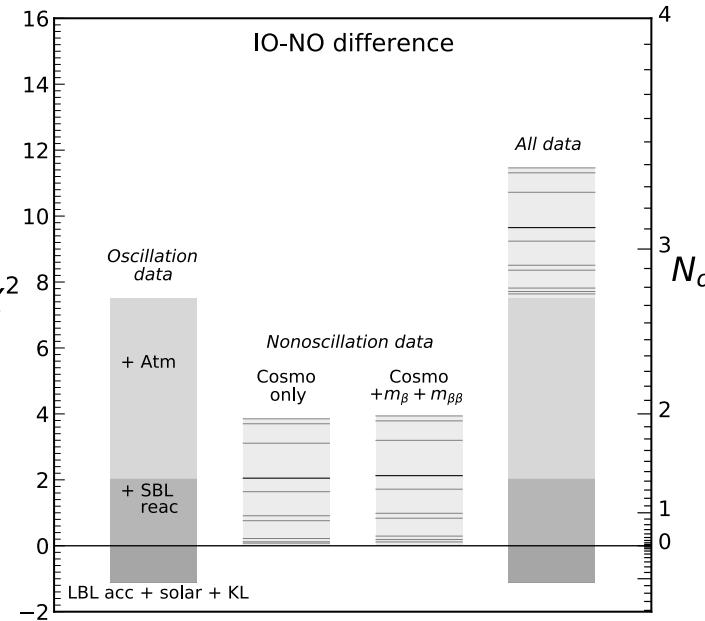
# Impact of cosmology on global oscillation fit, w.r.t. IO-NO difference

(envelope of conservative, default, aggressive case = horizontal lines)

arXiv:2003.08511 (pre v2020)



Update for this Colloquium



**Cosmo data may add from  $\sim 0$  to  $\sim 0.7\sigma$  to the  $\sim 2.7\sigma$  oscillation preference for NO  
→ overall typical  $\sim 3\sigma$  hint for NO vs IO**

Update of cosmological bounds with latest CMB data, and with emphasis on conservative cases wrt to possible future  $\beta$  and  $\beta\beta$  signals: in progress.

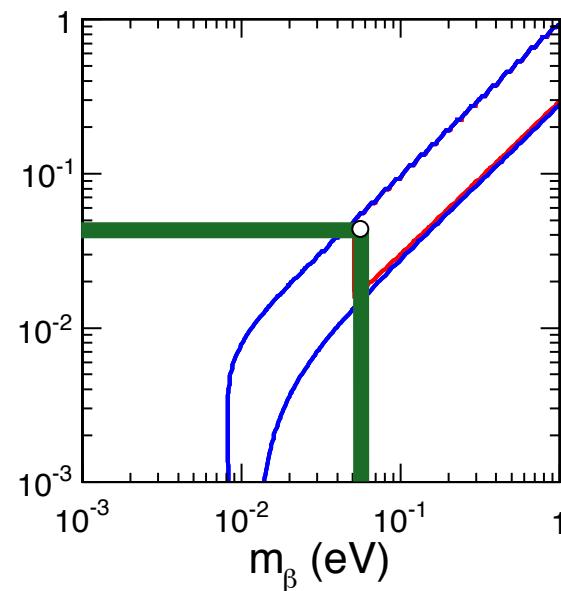
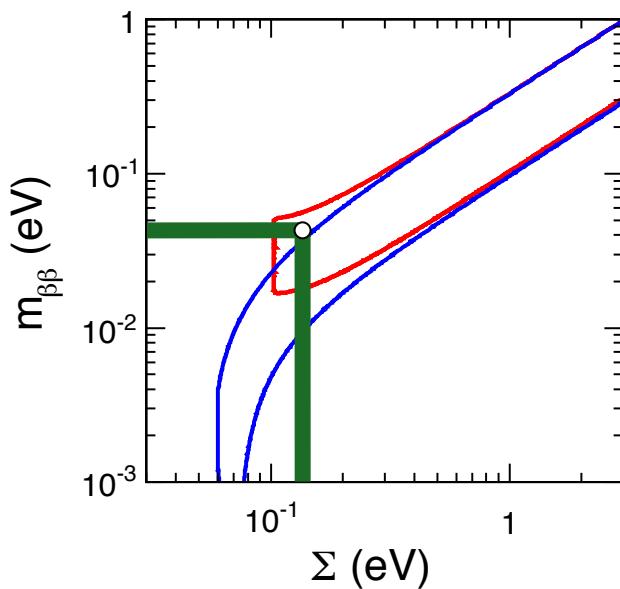
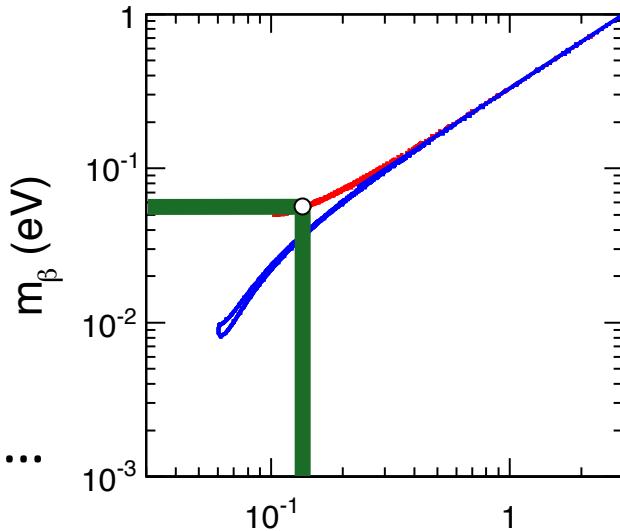
## Far future: with precise and converging non-oscillation signals one could...

Determine the mass scale...

Check  $3\nu$  consistency ...

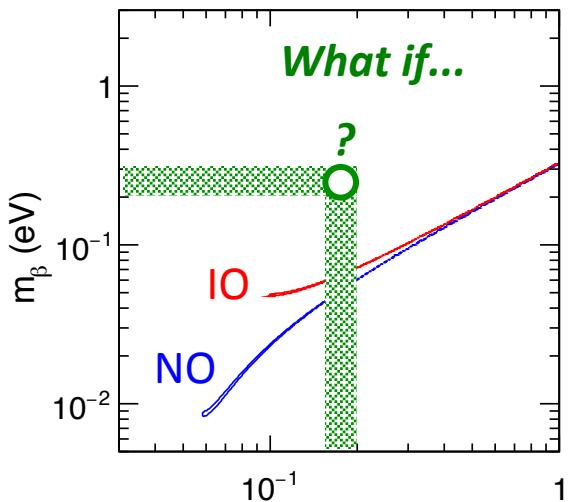
Identify the hierarchy ...

Probe the Majorana phase(s) ...

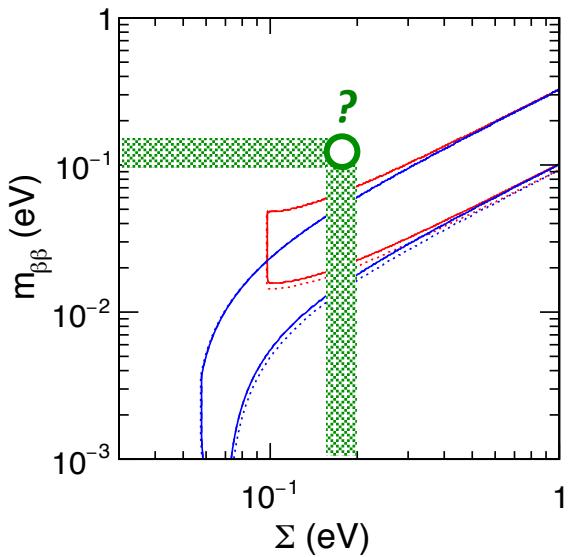


... but data might well bring us beyond 3 $\nu$  and re-shape the field!

Direct mass searches



Double beta decay



Cosmology

Lack of convergence among data  
(barring expt mistakes) might point  
towards new possibilities:

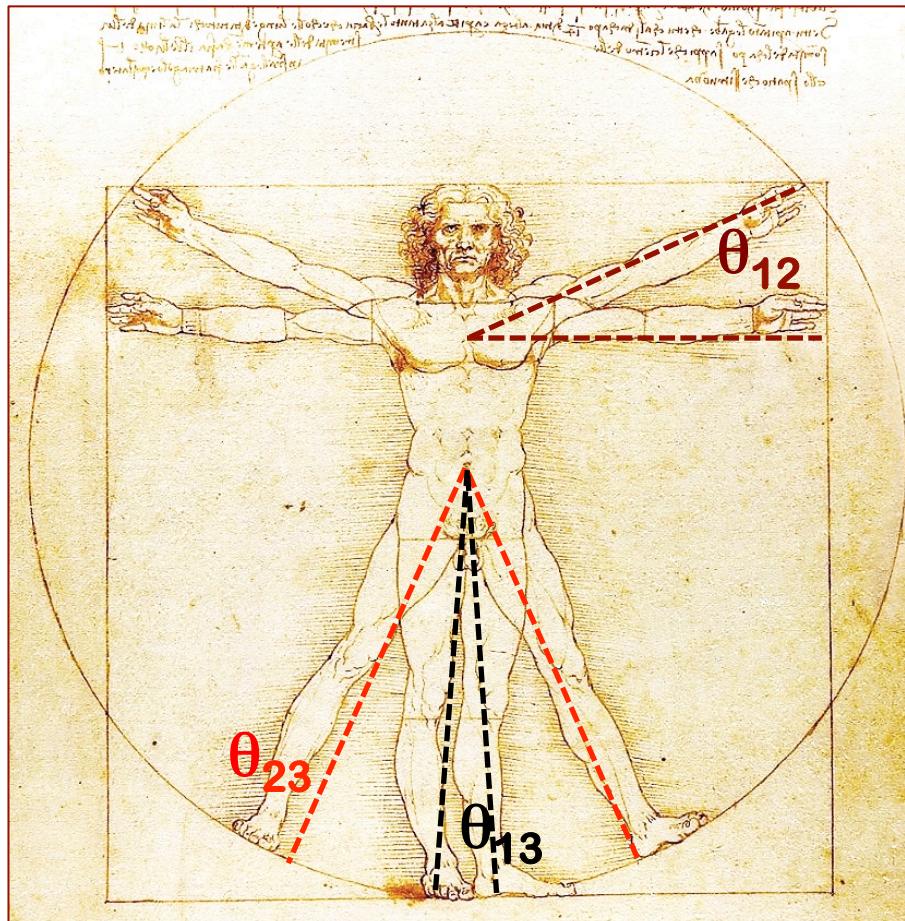
- Cosmology beyond  $\Lambda$ CDM
- New neutrino states
- New interactions
- Nonstandard  $\nu$  properties
- New phenomena in propagation
- ...

Main contender in current  $\nu$  physics:  
**Light sterile  $\nu$  at O(eV) scale**  
(Would require another colloquium...)

# Towards the epilogue...

- being excited by a series of discoveries
- charting the newly discovered territories
- trying to avoid distortions and biases
- seeking unknown lands and a bigger picture

## Mixings: are they suggestive of some “simmetry”...



...or the symmetry is only in our mind, and there is just randomness?

Many interesting ideas, but still looking for an “illumination”...

No organizing principle  
 (“anarchy”)



Discrete family symmetries  
 (“geometry”)

linear relations between  
 $\theta_{13} \cos \delta$  and  $\theta_{12}, \theta_{23}$

Continuous flavor symmetries  
 (“dynamics”)

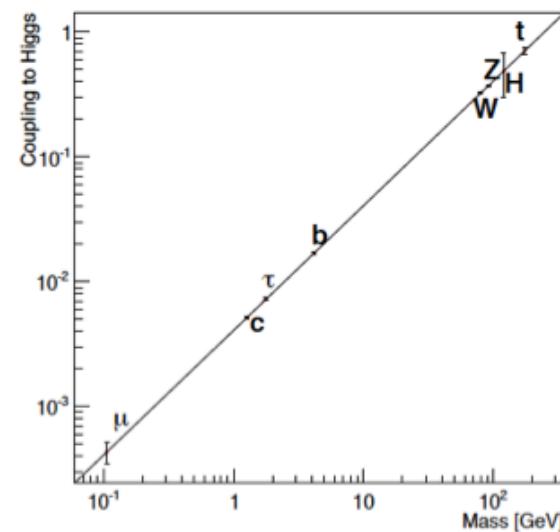
links between neutrino  
 masses/angles/phases

Common quark-lepton features  
 (“complementarity”)

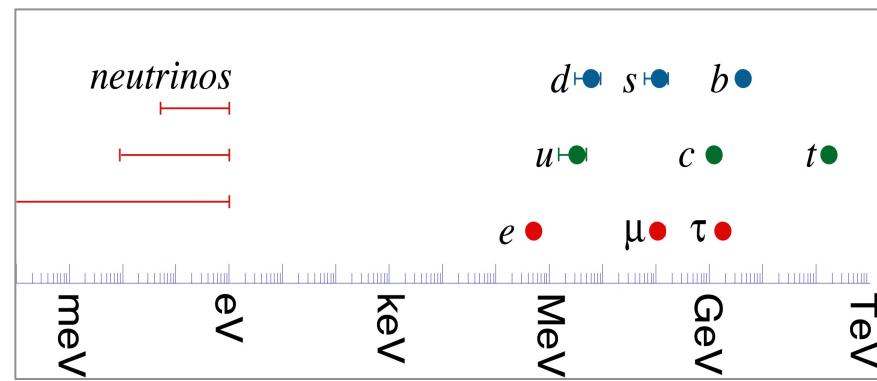
links between  
 $\theta_{13}$  and  $\theta_c$

# Masses: Linking two fundamental research expeditions

## 1. Test Higgs sector

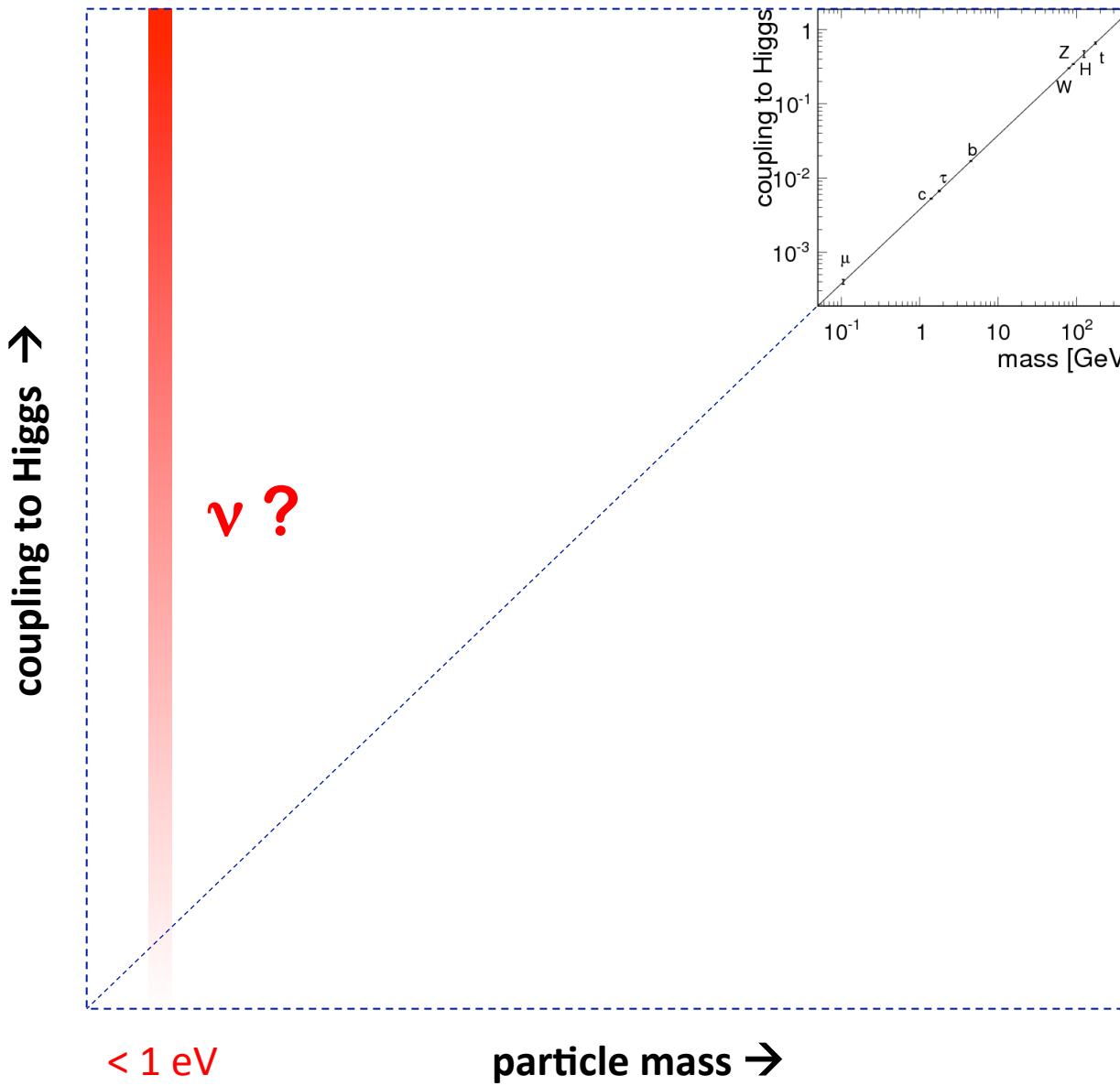


## 2. Fix $\nu$ masses



**1 + 2**

Where are the  $\nu$ 's on this plot? Why are they so light?



# Options:

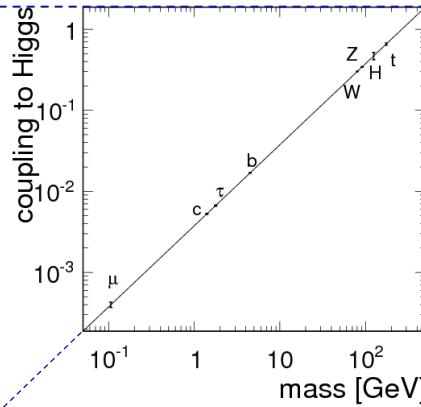
coupling to Higgs →

$\nu$

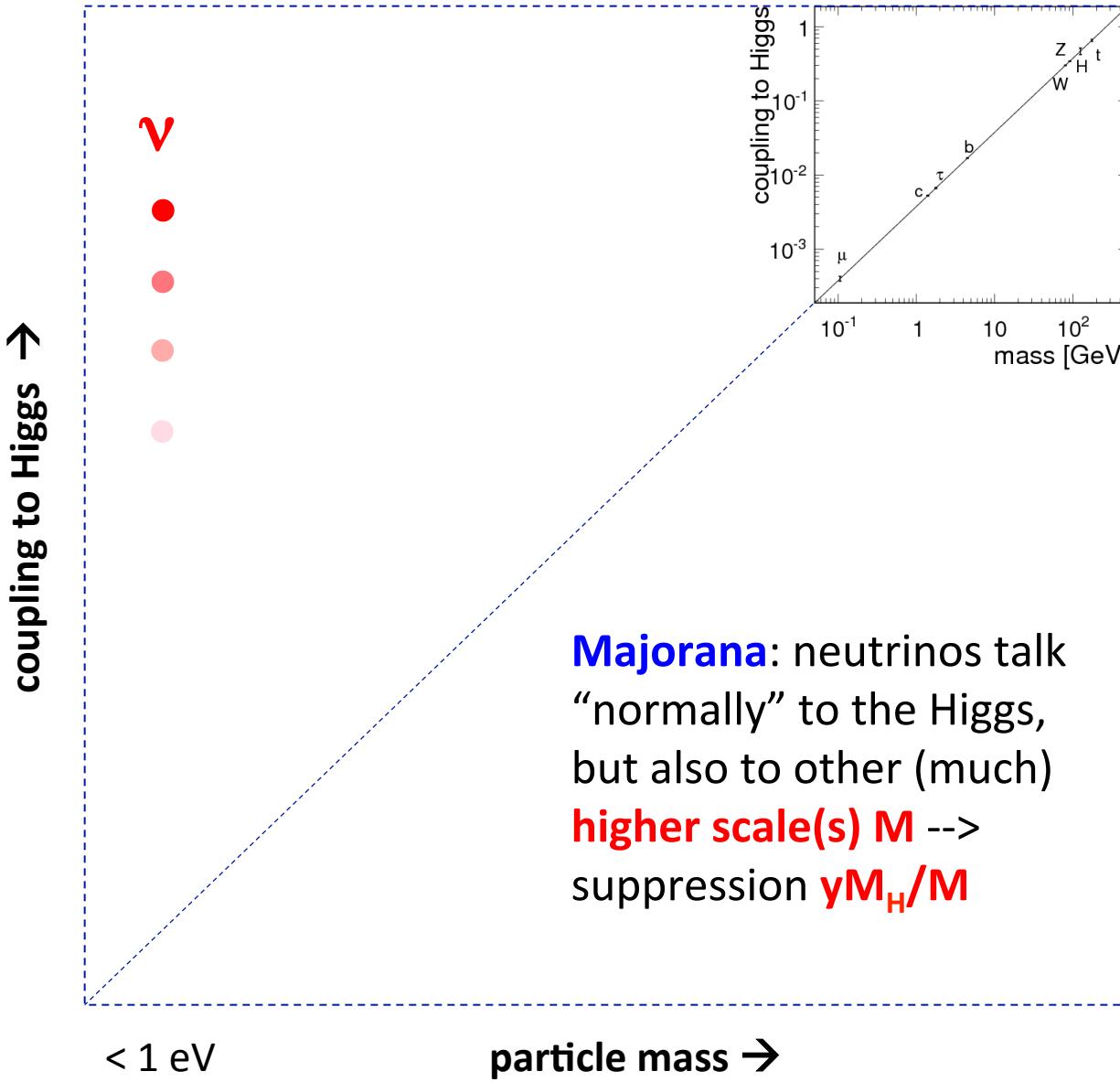
< 1 eV

particle mass →

**Dirac:** neutrinos “talk”  
very weakly to the  
Higgs boson,  $y < 10^{-12}$   
for unknown reasons...

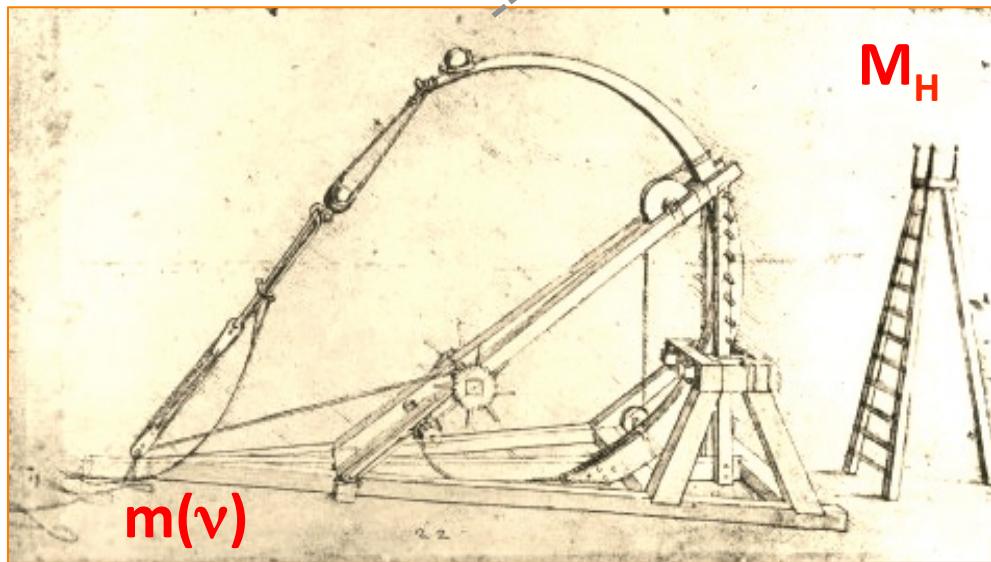


# Options:



**Neutrinos masses** may offer  
a great opportunity to jump  
**beyond the EW framework**  
via see-saw ...

M  
•  
•  
•  
•



... and to address fundamental physics issues, such as:

- new sources of CP violation at low and high energies
- lepton number violation and associated phenomena
- matter-antimatter asymmetry of the universe ...

$M \sim \text{GUT scale}$

CP-violating decays of heavy neutrinos at scale  
 $M$  may generate lepton asymmetry (leptogenesis):  
Discovery of leptonic CP violation and of Majorana nature (+ proton decay?) would be important steps towards this scenario.

- 
- 
- 
-

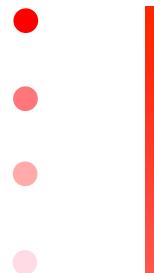
CP-violating decays of heavy neutrinos at scale  $M$  may generate lepton asymmetry (leptogenesis).  
Discovery of leptonic CP violation and of Majorana nature (+ proton decay?) would be important steps towards this scenario.



**$M \sim \text{low scale}$**

At the other end of the spectrum, low-scale (e.g. EW) see-saw may also generate (at the price of fine-tuning) additional interesting phenomenology: dark matter candidates, di-lepton and heavy lepton events in HEP

CP-violating decays of heavy neutrinos at scale  
M may generate lepton asymmetry (leptogenesis).  
**Discovery of leptonic CP violation and of Majorana nature (+ proton decay?) would be important steps towards this scenario.**



At the other end of the spectrum, low-scale (e.g. EW) see-saw may also generate (at the price of fine-tuning) additional interesting phenomenology: dark matter candidates, di-lepton and heavy lepton events in HEP

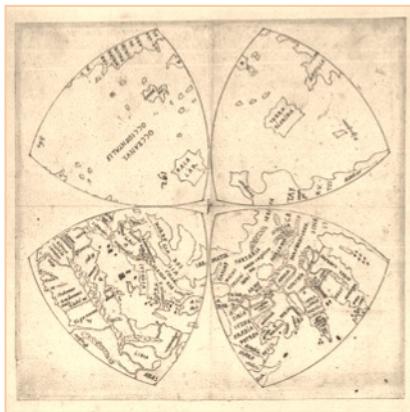
In principle, several sterile states might even be split among widely different energy scales, and affect various phenomena in (astro)particle physics.

**Let us remain open-minded!**

# Epilogue

$$\begin{aligned}\delta m^2 &\sim 8 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02\end{aligned}$$

*3v Terra Cognita...*



# Epilogue

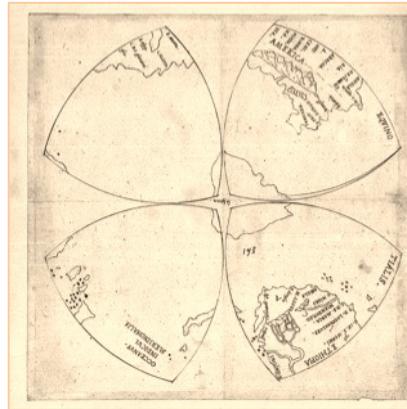
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$\delta$  (CP)  
 $\text{sign}(\Delta m^2)$   
 $\text{octant}(\theta_{23})$   
absolute masses  
Dirac/Majorana

*3v Terra Cognita...*



*3v Terra Incognita...*



# Epilogue

$$\begin{aligned}\delta m^2 &\sim 8 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02\end{aligned}$$

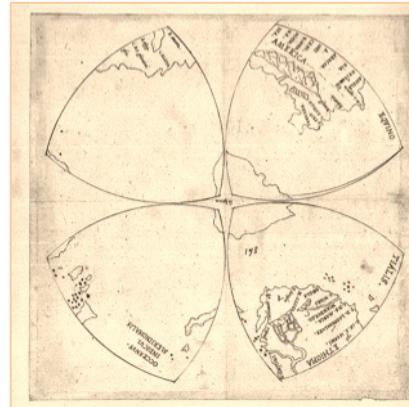
$\delta$  (CP)  
 $\text{sign}(\Delta m^2)$   
octant( $\theta_{23}$ )  
absolute masses  
Dirac/Majorana

new light states  
new interactions  
new heavy scales  
flavor structure  
origin of matter

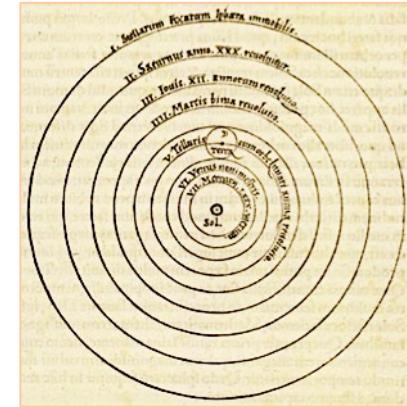
*3v Terra Cognita...*



*3v Terra Incognita...*



*... and beyond*



# Epilogue

$$\begin{aligned}\delta m^2 &\sim 7 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 &\sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} &\sim 0.3 \\ \sin^2 \theta_{23} &\sim 0.5 \\ \sin^2 \theta_{13} &\sim 0.02\end{aligned}$$

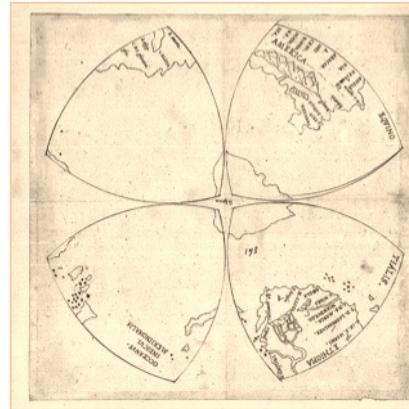
$\delta$  (CP)  
 $\text{sign}(\Delta m^2)$   
octant( $\theta_{23}$ )  
absolute masses  
Dirac/Majorana

new light states  
new interactions  
new heavy scales  
flavor structure  
origin of matter

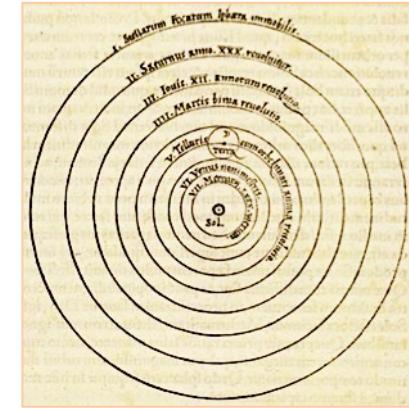
*3v Terra Cognita...*



*3v Terra Incognita...*



*... and beyond*



**Thank you for your attention**